

~~7775.5~~

~~7775.5~~

2

# NATIONAL ADVISORY COMMITTEE FOR AERONAUTICS

JUL 3 1947

## TECHNICAL MEMORANDUM

No. 1146

TEST REPORT ON THREE- AND SIX-COMPONENT MEASUREMENTS ON  
A SERIES OF TAPERED WINGS OF SMALL ASPECT RATIO

(Partial Report: Elliptic Wing)

By Lange/Wacke

Translation

“3- und 6-Komponentenmessung an der Zuspitzungsreihe  
von Flügeln kleiner Streckung. Teilbericht: Ellipsenflügel”

Deutsche Luftfahrtforschung, Untersuchungen und Mitteilungen Nr. 1023/3



Washington

June 1947

NACA LIBRARY  
LANGLEY MEMORIAL AERONAUTICAL  
LABORATORY  
Langley Field, Va.



3 1176 01437 4533

## NATIONAL ADVISORY COMMITTEE FOR AERONAUTICS

## TECHNICAL MEMORANDUM NO. 1146

TEST REPORT ON THREE- AND SIX-COMPONENT MEASUREMENTS  
ON A SERIES OF TAPERED WINGS OF  
SMALL ASPECT RATIO\*

(Partial Report: Elliptic Wing)

By Lange/Wacke

## INTRODUCTION

The report UM No. 1023/1 which presented the results of measurements for a series of trapezoidal wings was the beginning of a series on wings with aspect ratio 1 to 3 and various contours (fig. 1). In report No. 1023/1 the aspect ratio ( $\Lambda = 4/3$ ) remained the same; the tapering was modified. The present report gives the results of the series of elliptic wings. Here the aspect ratio varies from 1 to 2 with the sweepback. The contour is formed by elliptic arcs. (See fig. 2.)

The influence of sweepback and contour upon the neutral point is shown.

## MODELS

The models were made of wood at scale 1:1; the surface was polished. Three wings, identified as EE,  $\Lambda = 2$ ; DE,  $\Lambda = 4/3$ ; CE,  $\Lambda = 1$  were used. The dimensions and plan forms are given in figure 2. The elliptic-wing leading edge was produced by the affine distortion of an eighth circle. The airfoil was an NACA 0012 section.

---

\*"3- und 6-Komponentenmessung an der Zuspitzungsreihe von Flügeln kleiner Streckung, Teilbericht: Ellipsenflügel," Untersuchungen und Mitteilungen Nr. 1023/3. Zentrale für wissenschaftliches Berichtswesen der Luftfahrtforschung des Generalflugzeugmeisters (ZWB). Berlin-Adlershof, Sept. 21, 1943.

## APPARATUS AND METHODS

The tests were run in the  $3 \times 2.15$ m wind tunnel of the DVL. The models were suspended in the usual manner on the six-component balance. Care was taken to make the suspension conform to the test conditions of the preceding measurement, so as to ensure a good comparison of the results. The dynamic pressure was  $q = 100 \text{ kg/m}^2$  corresponding to 40 m/sec airspeed.

## COEFFICIENTS AND SYMBOLS

The forces and moments were measured with respect to the experimental system of axes (fig. 6).

The moment reference point for all three wings lies on the wing chord at a distance three-quarters of the mean reference chord from the wing trailing edge (fig. 2). The reference axes of the moments are defined as follows: (See fig. 6.)

Rolling moment:  $x_e$ -axis = line of intersection of the vertical plane of symmetry of the body with the horizontal plane of the tunnel (positive in wind direction).

Pitching moment:  $y_e$ -axis = lateral axis along the wing (positive toward the left, seen in wind direction).

Yawing moment:  $z_e$ -axis = normal axis in wind direction (positive downward).

All moments are positive when they are in a direction to produce clockwise rotation when looking along the positive direction of the axes.

The coefficients of the forces and moments are:

- A lift, kilograms
- W drag, kilograms
- Q cross-wind force, kilograms

L rolling moment

M pitching moment

N yawing moment

$$c_a = \frac{A}{q \times F} \quad \text{lift coefficient}$$

$$c_w = \frac{W}{q \times F} \quad \text{drag coefficient}$$

$$c_q = \frac{Q}{q \times F} \quad \text{cross-wind force coefficient}$$

$$c_L = \frac{L}{q \times F \times \frac{b}{2}} \quad \text{rolling-moment coefficient}$$

$$c_M = \frac{M}{q \times F \times l_m} \quad \text{pitching-moment coefficient}$$

$$c_N = \frac{N}{q \times F \times \frac{b}{2}} \quad \text{yawing-moment coefficient}$$

Angles:

$\alpha$  = angle of attack      angle between longitudinal axis  
along the wing and the  $x_e$ -axis

$\beta$  = angle of yaw      angle between the longitudinal axis  
in wind direction and the  $x_e$ -axis

The signs are for a right-hand positive system,  
clockwise rotation is positive.

Reference quantities:

F wing area, meters<sup>2</sup>

b span, meters

$l_m = \frac{F}{b}$  mean chord (reference chord), meters

$q = \frac{\rho}{2} v^2$  dynamic pressure, (kg/m<sup>2</sup>)

$\Lambda$  aspect ratio

Dimensions of models:

| Wing EE                  | Wing DE                 | Wing CE                 |
|--------------------------|-------------------------|-------------------------|
| $\Lambda = 2$            | $\Lambda = \frac{4}{3}$ | $\Lambda = 1$           |
| $F = 0.75 \text{ m}^2$   | $F = 0.75 \text{ m}^2$  | $F = 0.75 \text{ m}^2$  |
| $b = 1.225 \text{ m}$    | $b = 1 \text{ m}$       | $b = 0.866 \text{ m}$   |
| $l_m = 0.6125 \text{ m}$ | $l_m = 0.75 \text{ m}$  | $l_m = 0.866 \text{ m}$ |

## RESULTS

A list of the charts and tables is reproduced in table A.

(a) Three-component measurements.— The results are represented in graphs 1, 7, and 13 as  $c_a = f(\alpha)$ ,  $c_a = f(c_w)$ , and  $c_a = f(c_M)$ . The effectiveness of  $c_a'$  (slope of lift curve) decreases with decreasing  $\Lambda$  as expected. The increasing sweepback from wing EE to CE also acts in the decreasing sense.

At small angles of attack, the neutral point lies forward of the moment reference point; the wing is unstable. This forward position changes to a rearward position at higher  $c_a$  values. With increasing aspect ratio and increasing sweepback, the neutral point in the entire  $c_a$  range is moved back. The tuft measurements on the triangular wings indicated that the cause of it is attributable to a strong transverse flow in the rear part of the wing, which produces stabilizing lifting forces. With decreasing aspect ratio and increasing taper, the  $c_{a_{\max}}$  reaches a maximum value at  $\Lambda = 4/3$ .

where  $c_{a_{max}}$  shifts toward higher angles of attack.

Conspicuous is the sharp separation of flow on the wing  $\Lambda = 2$ , and the very flat curve in the range of  $c_{a_{max}}$  on the other two wings. This is mainly due to the sweepback, through which the additional velocity over the wing is substantially diminished.

(b) Six-component measurements.— The coefficients of the six-component measurements are presented with respect to the angle of yaw  $\beta$  and the angle of attack  $\alpha$  as parameter. The effect of the yawed flow on lift, drag, and pitching moment is small on all three wings. The cross-wind force is the same as on wings with large aspect ratio. At small  $\alpha$  a positive rise in cross-wind force with increasing  $\beta$  is observed, principally due to the form drag of the leading-wing leading edge. It is greatest at the wings with least sweepback (wing EE). At greater angles of attack the negative cross-wind force of the wing predominates. The cross-wind force curve of DE,  $\Lambda = 4/3$ , deviates from this variation at  $\alpha = 35.47^\circ$  ( $c_{a_{max}}$ ).

The rolling moment increases with sweepback as a result of the transverse flow in the rear part of the wing.

The yawing-moment variation with the angle of yaw is negative for all three wings. With increasing angle of attack, the directional stability increases. This is also dependent upon the form drag of the leading edge of the wing.

#### ADDITIONAL REPORTS OF THE SERIES

|                                       | UM NO. |
|---------------------------------------|--------|
| Trapezoidal wing ( $\Lambda = 4/3$ )  | 1023/1 |
| Trapezoidal wing with fuselage        | 1023/2 |
| Elliptical wing with fuselage         | 1023/4 |
| Triangular wing ( $\Lambda = 3 - 1$ ) | 1023/5 |
| Triangular wing with fuselage         | 1023/6 |

Voepel, DFS, of the firm of Henschel, Schönefeld, is preparing a summary of all results of this series of measurements taking the theory of wings of small aspect ratio into consideration.

Translated by J. Vanier  
National Advisory Committee  
for Aeronautics

TABLE A

SURVEY OF THE THREE- AND SIX-COMPONENT MEASUREMENTS  
ON THE SERIES OF TAPERED WING (ELLIPTIC WING)

| Symbol                                |                                | Angle                |               | Chart of<br>curves | Table |
|---------------------------------------|--------------------------------|----------------------|---------------|--------------------|-------|
|                                       |                                | $\alpha^\circ$       | $\beta^\circ$ |                    |       |
| EE<br>$\Lambda = 2$                   | Three-component<br>measurement | Variable             | 0             | 1                  | 1     |
|                                       | Six-component<br>measurement   | 0                    | Variable      | 2                  | 2     |
|                                       | Do----                         | 6.84                 | ---do---      | 3                  | 2     |
|                                       | Do----                         | 13.87                | ---do---      | 4                  | 3     |
|                                       | Do----                         | 20.51                | ---do---      | 5                  | 3     |
|                                       | Do----                         | 23.79                | ---do---      | 6                  | 4     |
| DE<br>$\Lambda = \frac{4}{3}$         | Three-component<br>measurement | Variable             | 0             | 7                  | 5     |
|                                       | Six-component<br>measurement   | 0                    | Variable      | 8                  | 6     |
|                                       | Do----                         | 9.43                 | ---do---      | 9                  | 6     |
|                                       | Do----                         | 17.95                | ---do---      | 10                 | 7     |
|                                       | Do----                         | 25.89                | ---do---      | 11                 | 7     |
|                                       | Do----                         | 35.47                | ---do---      | 12                 | 8     |
| CE<br>$\Lambda = 1$                   | Three-component<br>measurement | Variable             | 0             | 13                 | 9     |
|                                       | Six-component<br>measurement   | 0.4                  | Variable      | 14                 | 10    |
|                                       | Do----                         | 11.73                | ---do---      | 15                 | 10    |
|                                       | Do----                         | 21.36                | ---do---      | 16                 | 11    |
|                                       | Do----                         | 30.30                | ---do---      | 17                 | 11    |
|                                       | Do----                         | 38.63                | ---do---      | 18                 | 12    |
| Comparative curves of the three wings |                                |                      |               |                    |       |
| $c_a = f(\alpha); c_a = f(c_w)$       |                                | Variable             | 0             | 19                 |       |
| $c_a = f(c_M)$                        |                                | Variable             | 0             | 20                 |       |
| $c_L$ and $c_q = f(\beta)$            |                                | $\alpha_{c_a} = 0.3$ | Variable      | 21                 |       |
| $c_L$ and $c_q = f(\beta)$            |                                | $\alpha_{c_a} = 0.9$ | Variable      | 22                 |       |



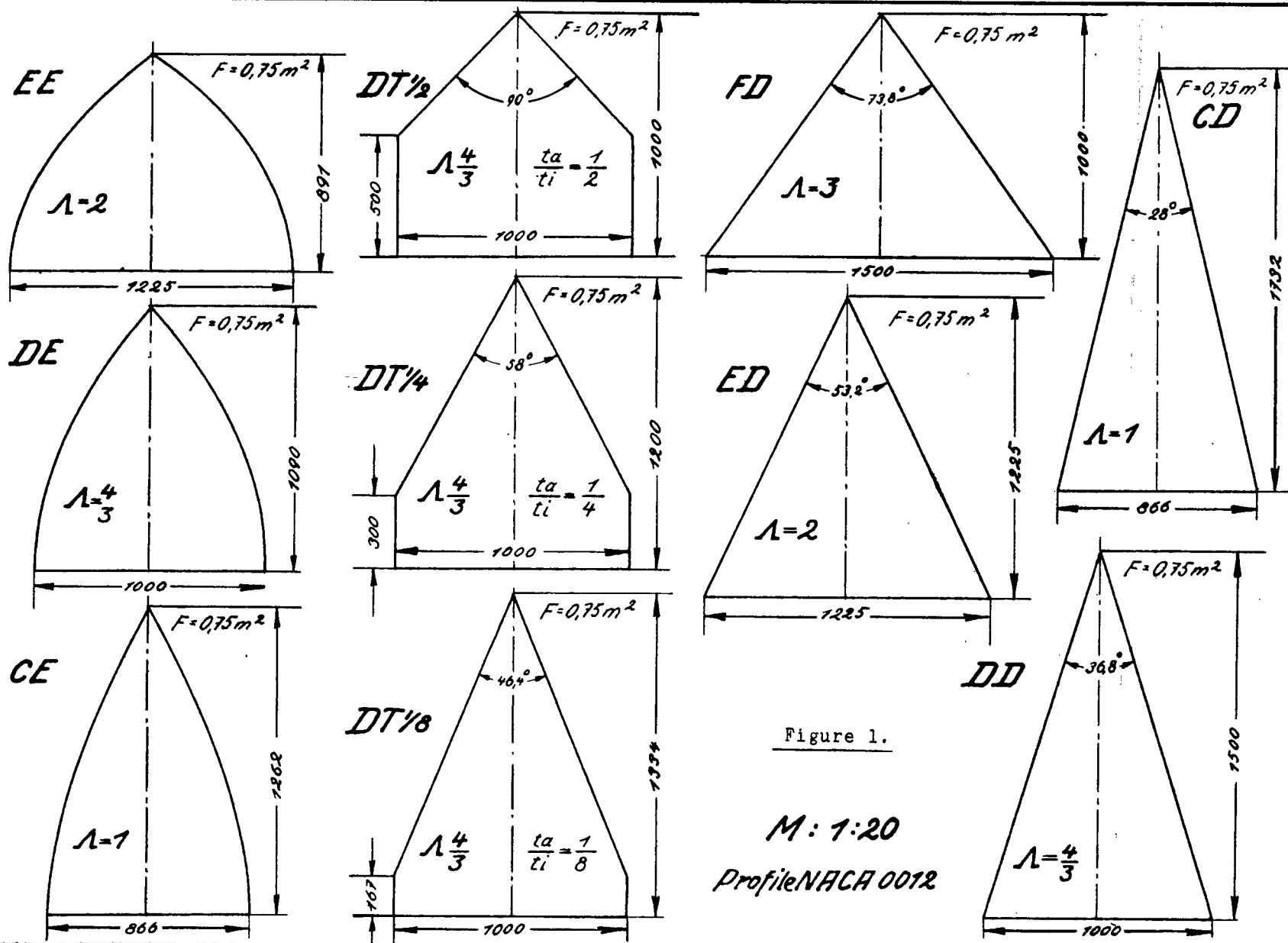


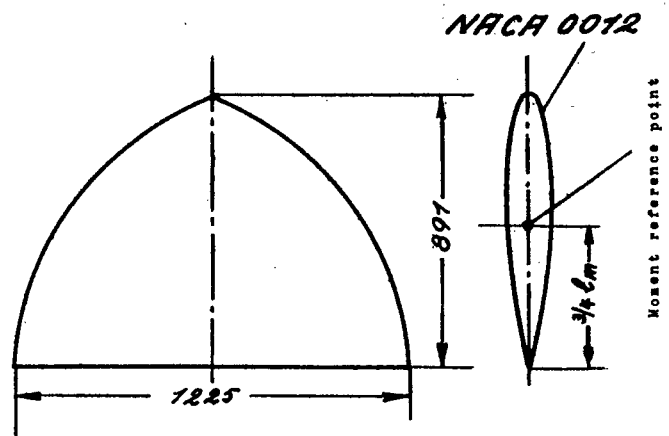
Figure 1.

$M: 1:20$   
 Profile NACA 0012

Figure 2.  
Elliptic wing

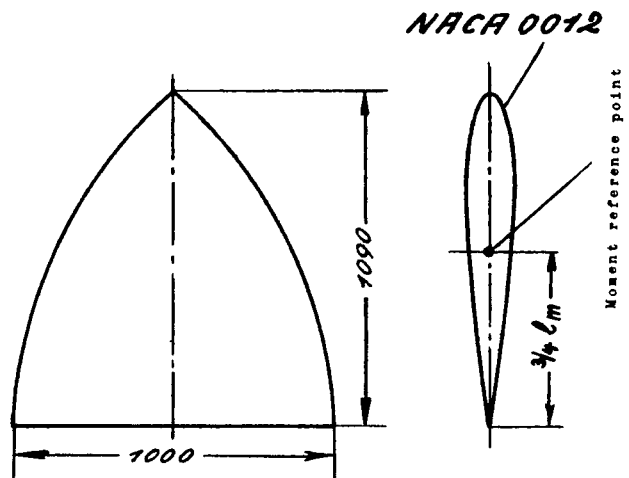
**EE**

$$\begin{aligned}\Lambda &= 2 \\ F &= 0,75 \text{ m}^2 \\ b &= 1,225 \text{ m} \\ l_m &= \frac{F}{b} = 0,6125 \text{ m}\end{aligned}$$



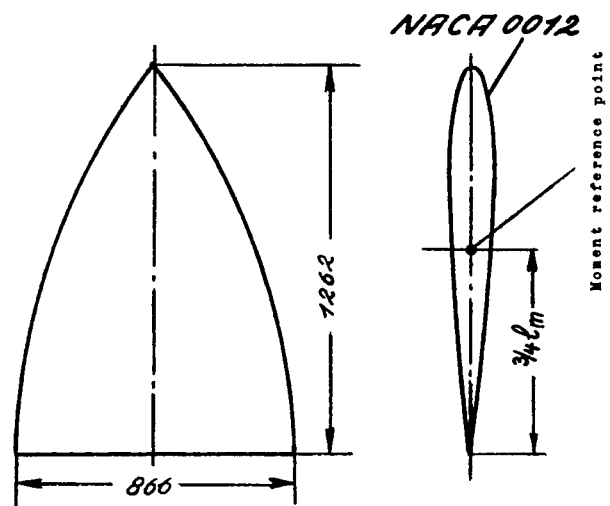
**DE**

$$\begin{aligned}\Lambda &= \frac{4}{3} \\ F &= 0,75 \text{ m}^2 \\ b &= 1 \text{ m} \\ l_m &= \frac{F}{b} = 0,75 \text{ m}\end{aligned}$$



**CE**

$$\begin{aligned}\Lambda &= 1 \\ F &= 0,75 \text{ m}^2 \\ b &= 0,866 \text{ m} \\ l_m &= \frac{F}{b} = 0,866 \text{ m}\end{aligned}$$



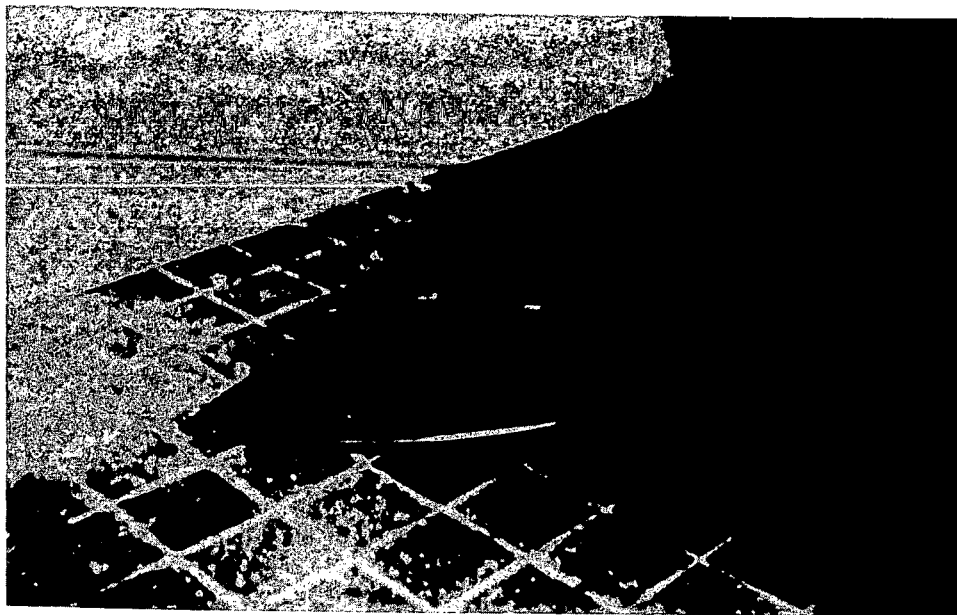


Figure 3.  
Wing EE,  $\Lambda = 2$



Figure 4.  
Wing DE,  $\Lambda = 4/3$

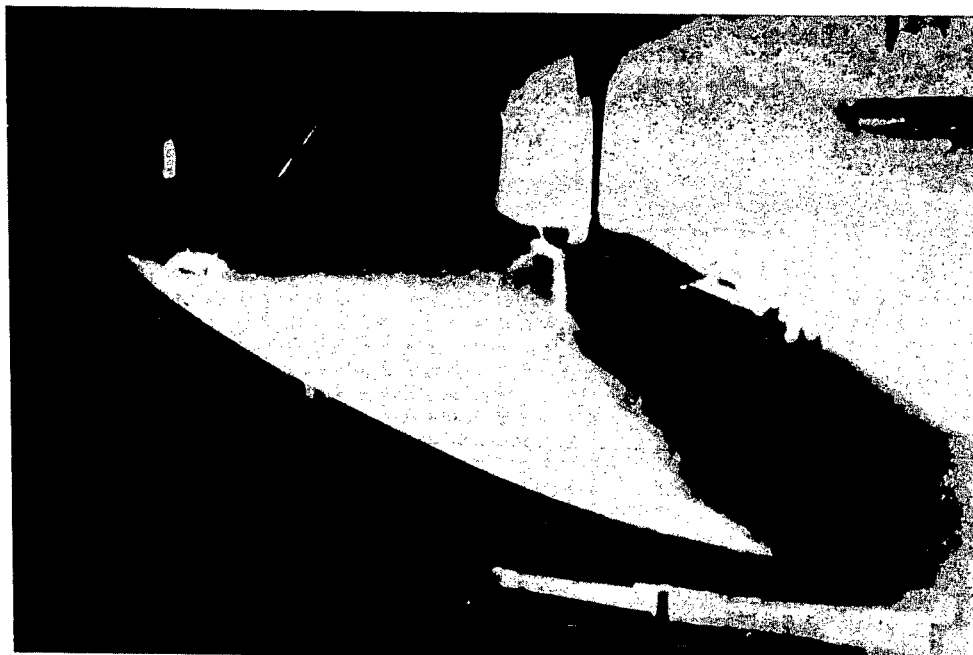


Figure 5.  
Wing CE,  $\Lambda=1$   
in 2.15x 3m windtunnel

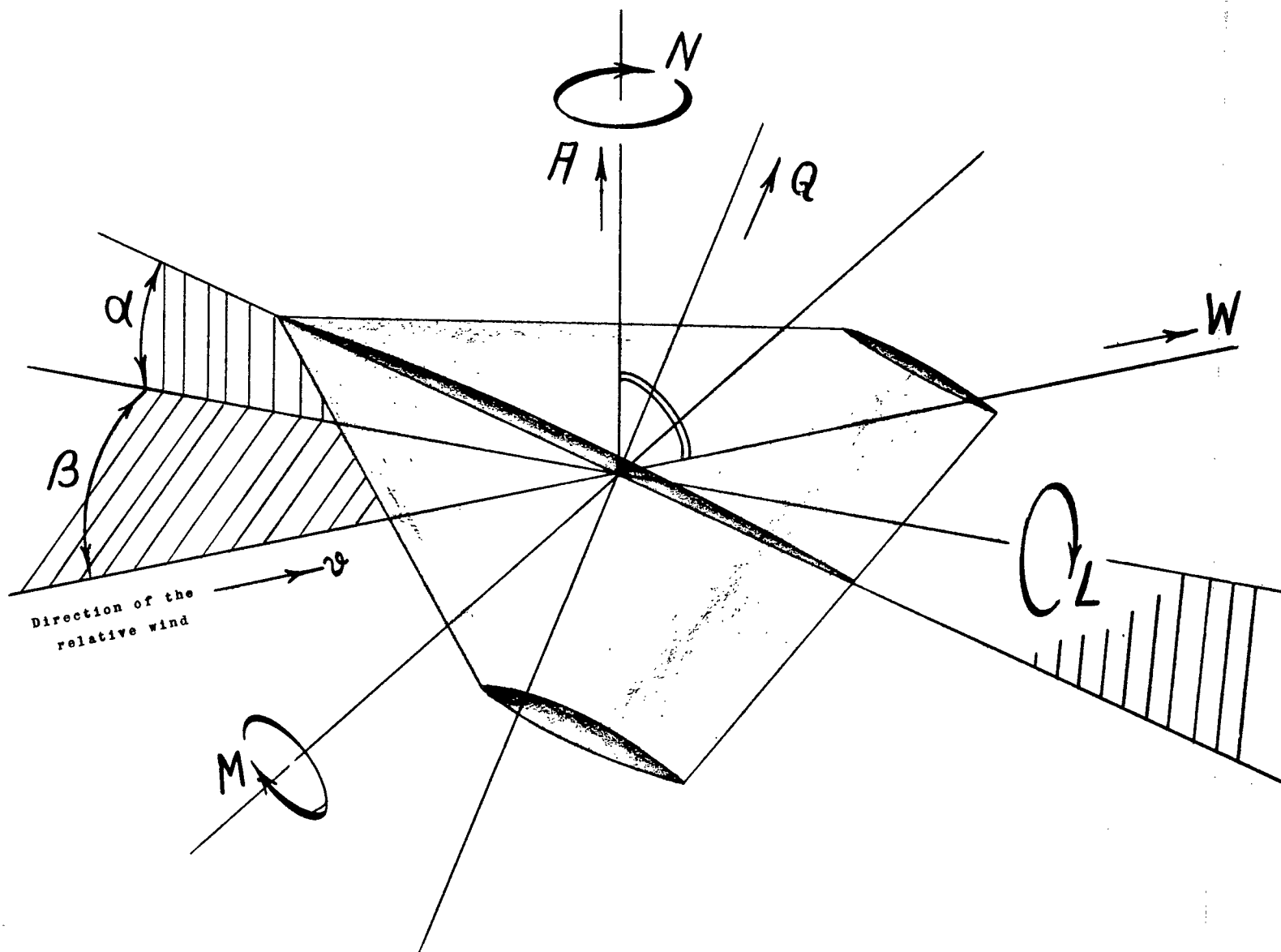


Figure 6. Coordinate system of the 6-component measurement.

THREE-COMPONENT MEASUREMENTS OF A SERIES OF TAPERED WINGS  
 (Elliptic Wing)  
 TABLE NO. 1 TO CHART 1  
 $EE, \Lambda = 2$

| $\alpha^\circ$ | $c_a$       | $c_w$  | $c_M$   |
|----------------|-------------|--------|---------|
| -5.70          | -0.2412     | 0.0175 | -0.0176 |
| 0              | 0           | .0061  | .0009   |
| 5.69           | .2480       | .0180  | .0188   |
| 11.39          | .4950       | .0502  | .0321   |
| 17.08          | .7460       | .1067  | .0343   |
| 19.91          | .8790       | .1515  | .0309   |
| 22.75          | 1.0110      | .2097  | .0227   |
| 23.70          | 1.0520      | .2323  | .0225   |
| 24.17          | 1.0780      | .2429  | .0203   |
| 24.64          | 1.0990      | .2560  | .0193   |
| 25.10          | 1.12-1.135  | .3285  | .0201   |
| 25.82          | 0.947-0.966 | .4182  | -.0049  |
| 26.94          | 0.827-0.88  | .4273  | -.0191  |
| 0              | .0027       | .0060  | .0013   |

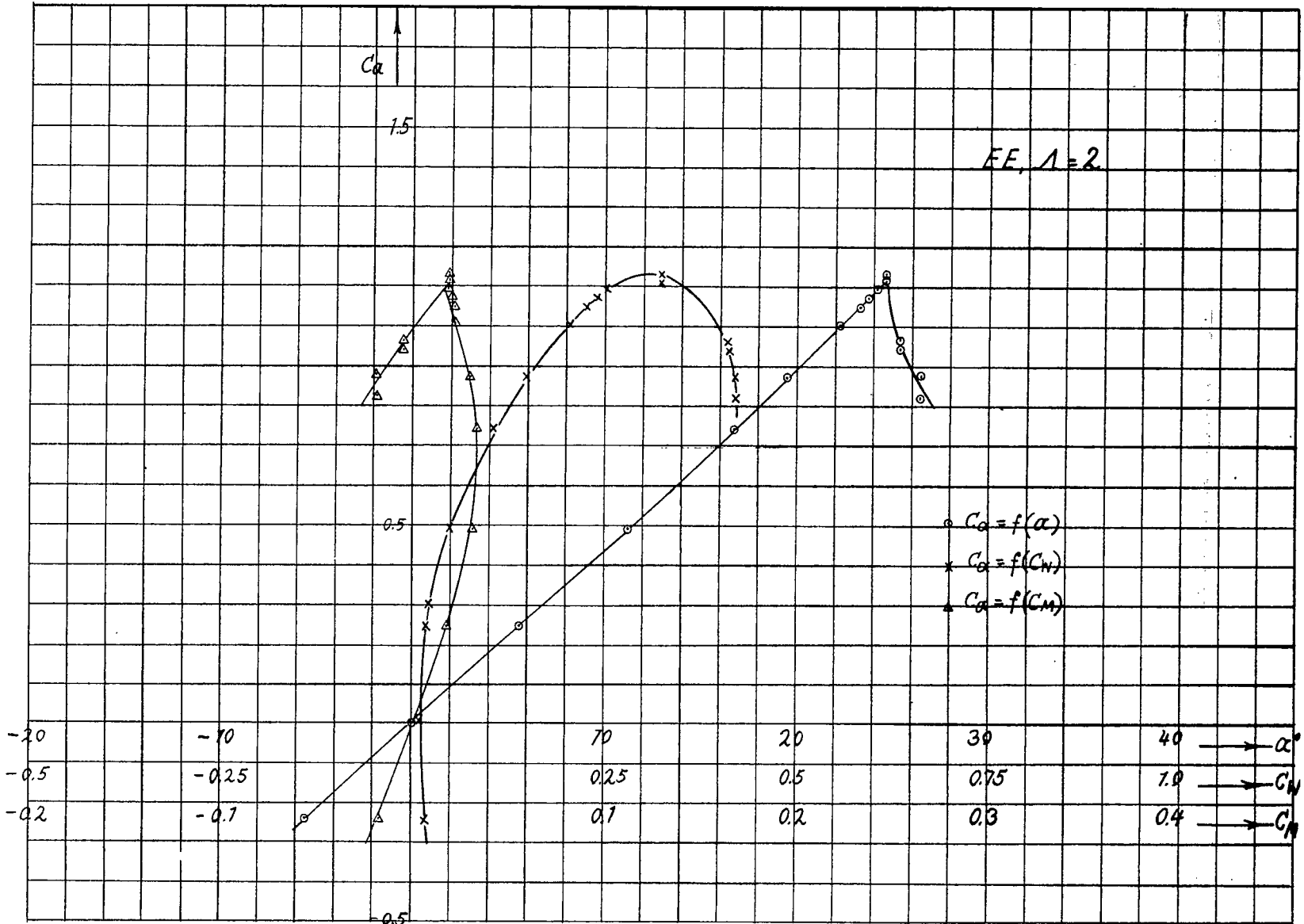


Chart 1. 3 - component measurements of a series of tapered wings (elliptic wing)  
Table 1.

SIX-COMPONENT MEASUREMENTS OF A SERIES OF TAPERED WINGS  
(Elliptic Wing)

TABLE NO. 2 TO CHARTS 2,3

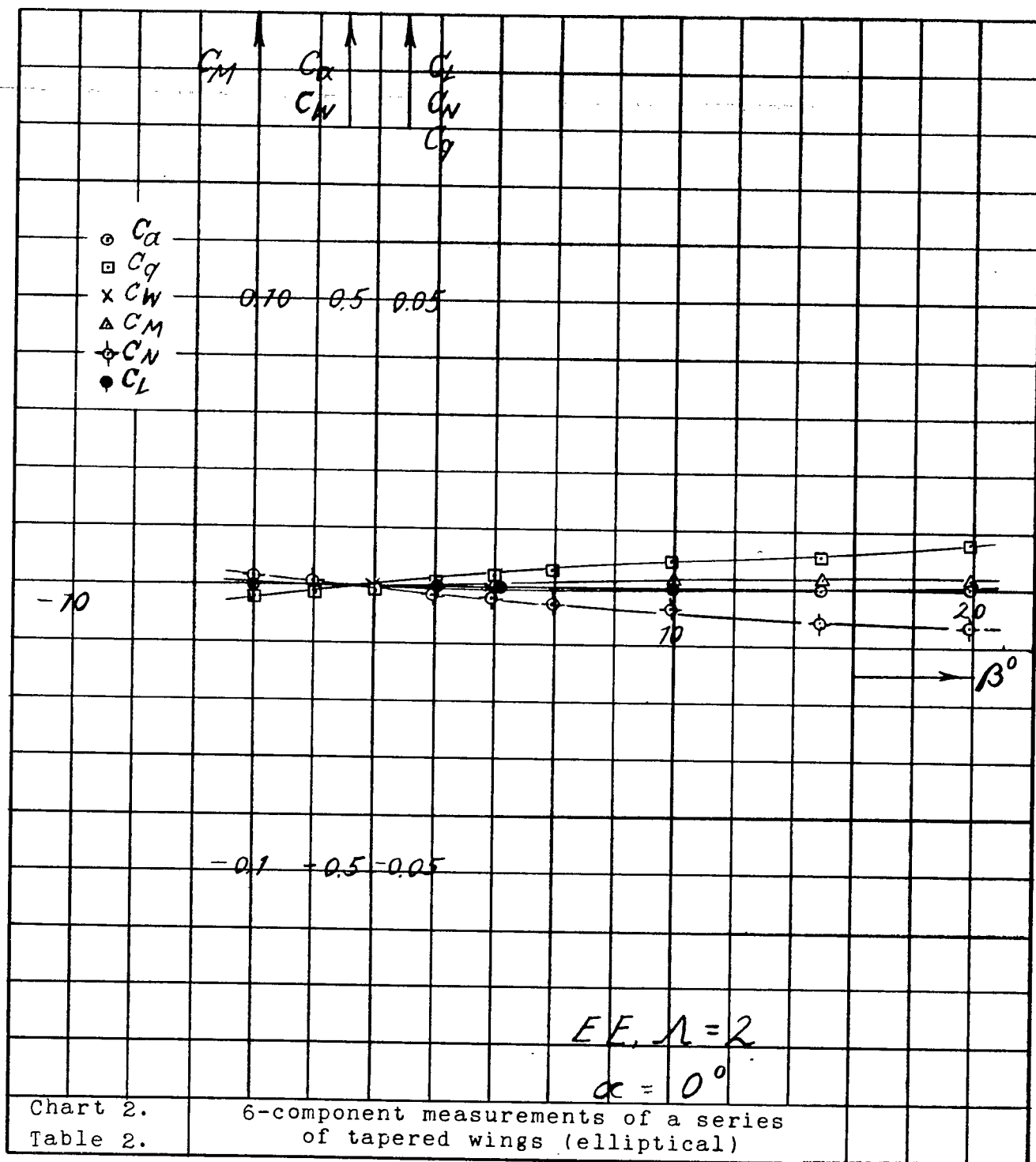
EE,  $\Lambda = 2$  $\alpha = 0$ 

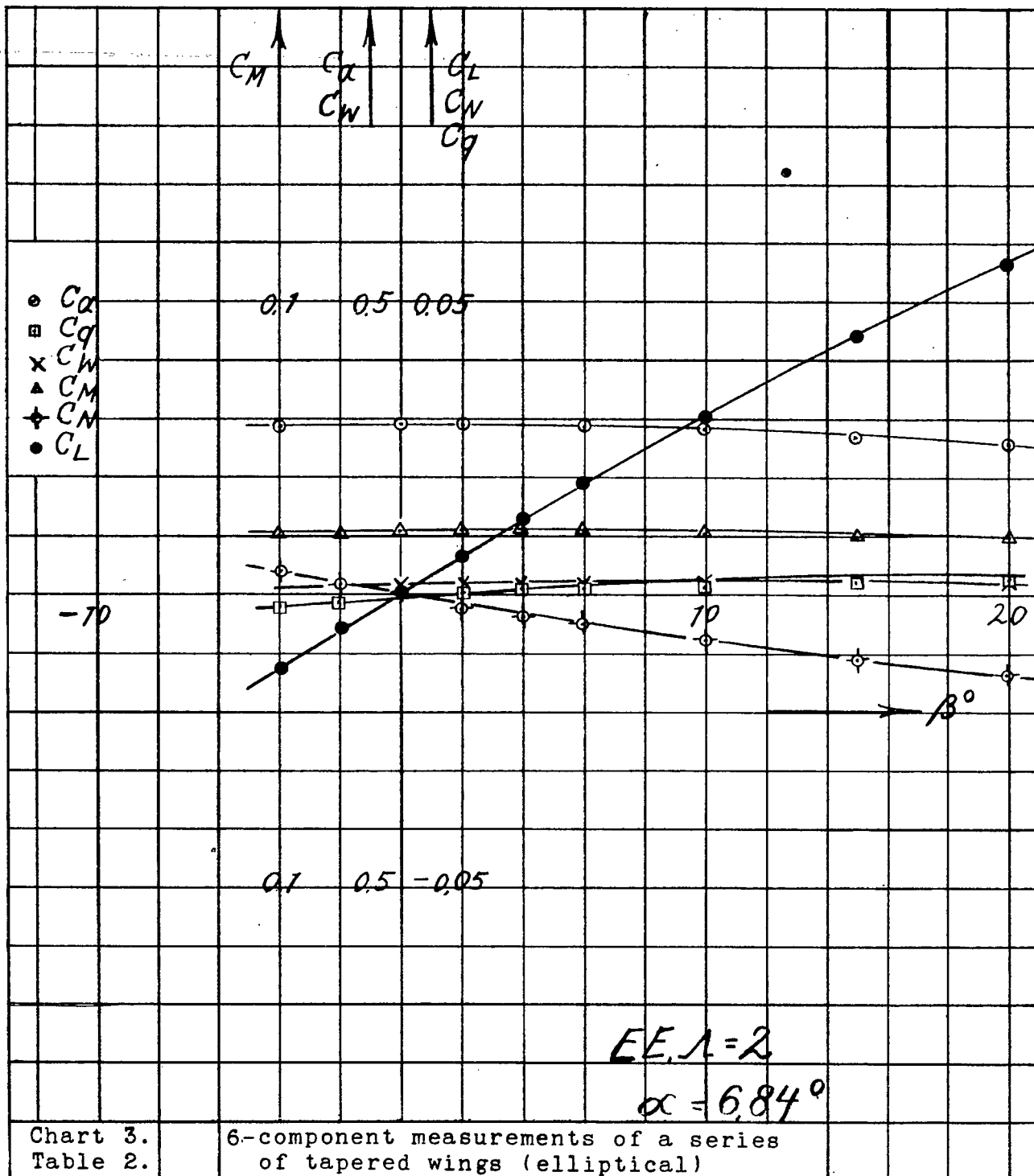
| $\beta^\circ$ | $c_a$  | $c_q$   | $c_w$  | $c_L$  | $c_M$  | $c_N$  |
|---------------|--------|---------|--------|--------|--------|--------|
| -4            | 0.0030 | -0.0020 | 0.0063 | 0      | 0.0014 | 0.0020 |
| -2            | .0030  | -.0013  | .0063  | -.0001 | .0014  | .0007  |
| 0             | .0030  | 0       | .0063  | 0      | .0014  | 0      |
| 2             | .0030  | .0013   | .0063  | .0001  | .0014  | -.0010 |
| 4             | .0030  | .0027   | .0063  | 0      | .0014  | -.0021 |
| 6             | .0030  | .0033   | .0063  | .0001  | .0014  | -.0026 |
| 10            | .0030  | .0047   | .0072  | .0009  | .0014  | -.0036 |
| 15            | .0030  | .00600, | .0081  | .0010  | .0014  | -.0053 |
| 20            | .0030  | .0080   | .0093  | .0017  | .0015  | -.0062 |

EE,  $\Lambda = 2$  $\alpha = 6.84^\circ$ 

| $\beta^\circ$ | $c_a$  | $c_q$   | $c_w$  | $c_L$   | $c_M$  | $c_N$  |
|---------------|--------|---------|--------|---------|--------|--------|
| -4            | 0.2960 | -0.0020 | 0.0221 | -0.0128 | 0.0220 | 0.0041 |
| -2            | .2960  | -.0013  | .0223  | -.0060  | .0221  | .0024  |
| 0             | .2960  | -.0007  | .0221  | 0       | .0230  | .0003  |
| 2             | .2960  | .0007   | .0221  | .0069   | .0224  | -.0021 |
| 4             | .2960  | .0013   | .0221  | .0129   | .0221  | -.0035 |
| 6             | .2940  | .0013   | .0221  | .0197   | .0223  | -.0046 |
| 10            | .2860  | .0017   | .0222  | .0304   | .0226  | -.0076 |
| 15            | .2740  | .0023   | .0226  | .0448   | .0216  | -.0111 |
| 20            | .2620  | .0030   | .0227  | .0569   | .0199  | -.0140 |







SIX-COMPONENT MEASUREMENTS OF A SERIES OF TAPERED WINGS  
(Elliptic Wing)

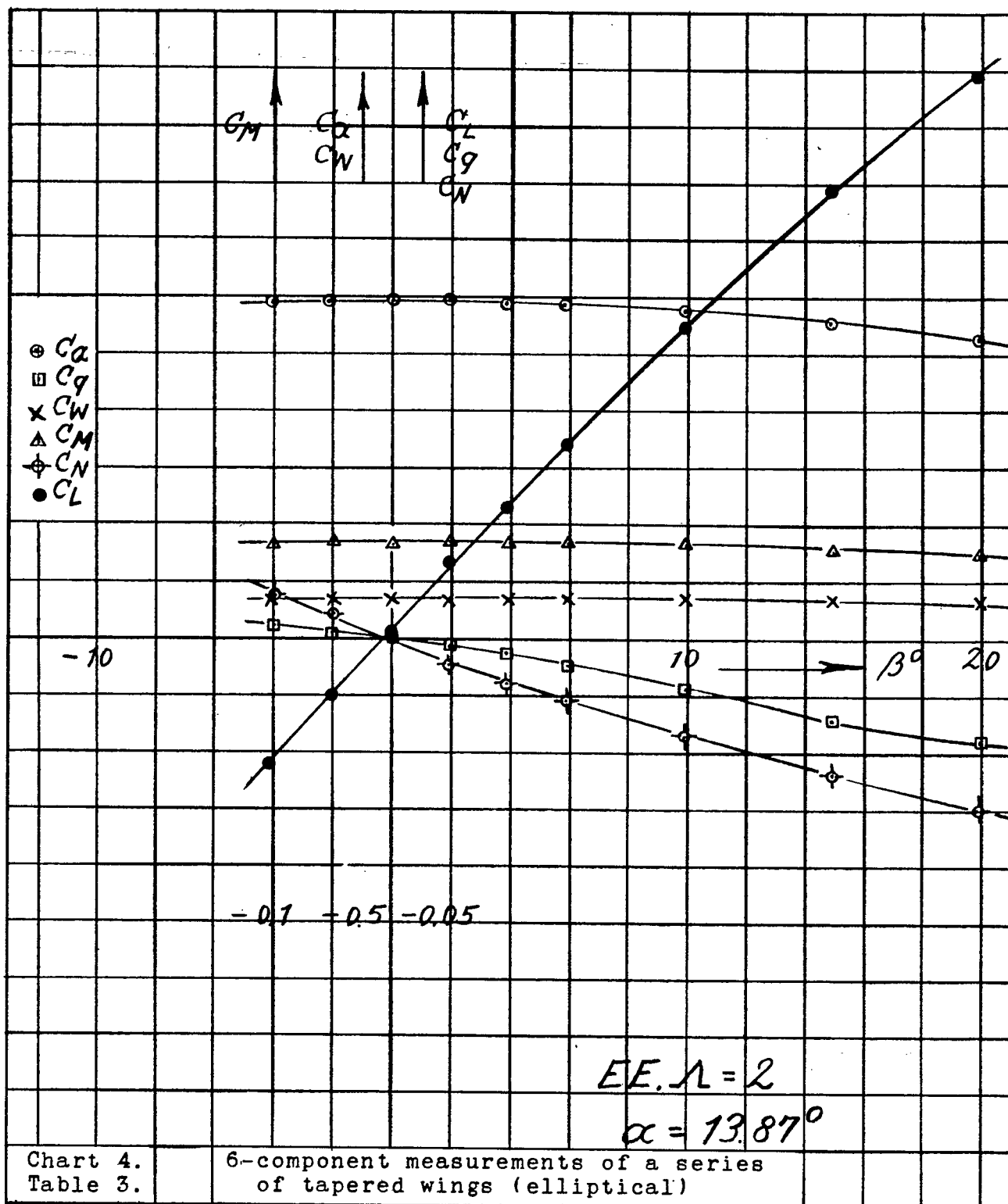
TABLE NO. 3 TO CHARTS 4, 5

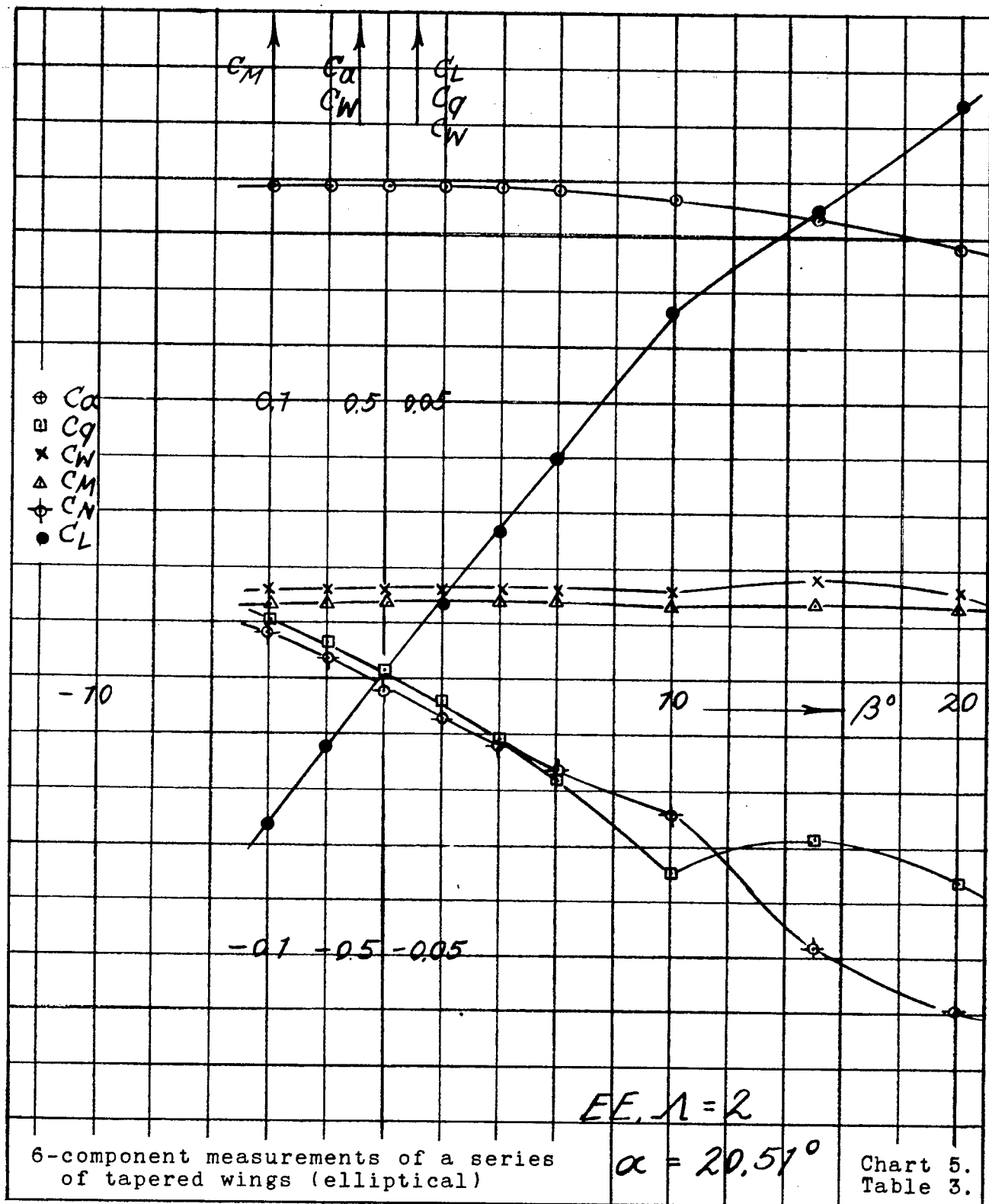
EE,  $\Lambda = 2$  $\alpha = 13.87^\circ$ 

| $\beta^\circ$ | $c_a$ | $c_q$  | $c_w$  | $c_L$   | $c_M$  | $c_N$  |
|---------------|-------|--------|--------|---------|--------|--------|
| -4            | 0.601 | 0.0027 | 0.0731 | -0.0219 | 0.0340 | 0.0081 |
| -2            | .602  | .0013  | .0732  | -.0098  | .0347  | .0040  |
| 0             | .604  | .0003  | .0730  | .0015   | .0346  | -.0002 |
| 2             | .602  | -.0013 | .0731  | .0136   | .0347  | -.0049 |
| 4             | .600  | -.0027 | .0730  | .0235   | .0341  | -.0081 |
| 6             | .596  | -.0047 | .0726  | .0348   | .0344  | -.0110 |
| 10            | .585  | -.0087 | .0712  | .0554   | .0334  | -.0171 |
| 15            | .564  | -.0147 | .0692  | .0799   | .0320  | -.0241 |
| 20            | .536  | -.0186 | .0674  | .1004   | .0300  | -.0307 |

EE,  $\Lambda = 2$  $\alpha = 20.51^\circ$ 

| $\beta^\circ$ | $c_a$ | $c_q$  | $c_w$  | $c_L$   | $c_M$  | $c_N$  |
|---------------|-------|--------|--------|---------|--------|--------|
| -4            | 0.903 | 0.0107 | 0.1642 | -0.0265 | 0.0275 | 0.0116 |
| -2            | .904  | .0067  | .1643  | -.0123  | .0284  | .0046  |
| 0             | .905  | .0020  | .1643  | .0014   | .0289  | -.0022 |
| 2             | .905  | -.0040 | .1644  | .0136   | .0289  | -.0070 |
| 4             | .901  | -.0113 | .1645  | .0274   | .0293  | -.0118 |
| 6             | .896  | -.0180 | .1639  | .0405   | .0288  | -.0166 |
| 10            | .884  | -.0346 | .1623  | .0674   | .0277  | -.0240 |
| 15            | .850  | -.0286 | .1688  | .0858   | .0280  | -.0487 |
| 20            | .794  | -.0366 | .1623  | .1056   | .0279  | -.0604 |



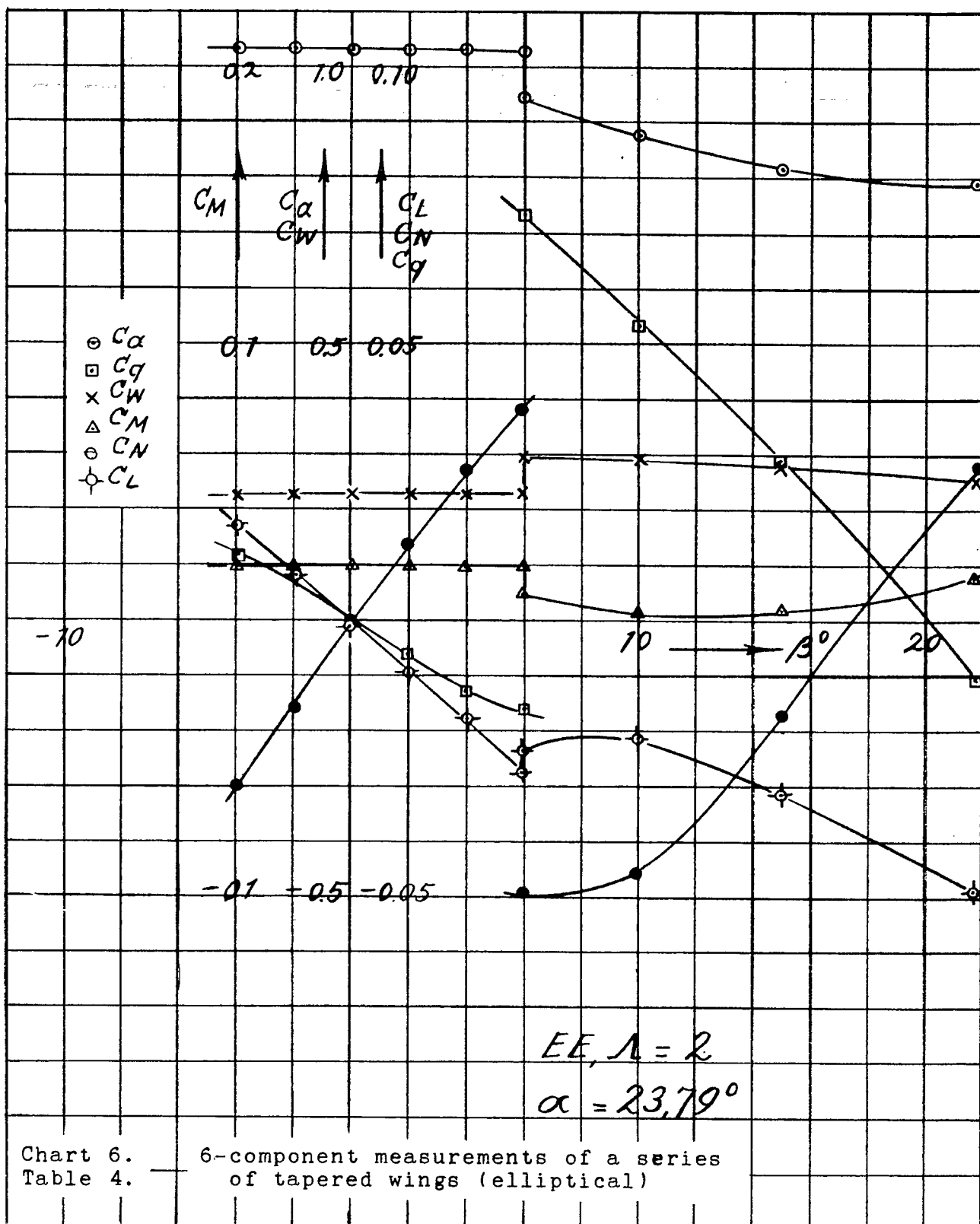


SIX-COMPONENT MEASUREMENTS OF A SERIES OF TAPERED WINGS  
(Elliptic Wing)

TABLE NO. 4 TO CHART 6

EE,  $\Lambda = 2$  $\alpha = 23.79^\circ$ 

| $\beta^\circ$ | $c_a$ | $c_q$  | $c_w$  | $c_L$   | $c_M$  | $c_N$  |
|---------------|-------|--------|--------|---------|--------|--------|
| -4            | 1.050 | 0.0120 | 0.2322 | -0.0302 | 0.0208 | 0.0176 |
| -2            | 1.051 | .0073  | .2317  | -.0167  | .0207  | .0083  |
| 0             | 1.052 | 0      | .2320  | -.0008  | .0209  | -.0008 |
| 2             | 1.054 | -.0060 | .2331  | .0144   | .0206  | -.0092 |
| 4             | 1.051 | -.0127 | .2351  | .0279   | .0211  | -.0178 |
| 6             | 1.045 | -.0160 | .2384  | .0390   | .0217  | -.0279 |
| 6             | .965  | .0746  | .3012  | -.0492  | .0119  | -.0239 |
| 10            | .898  | .0546  | .2998  | -.0455  | .0046  | -.0213 |
| 15            | .831  | .0300  | .2856  | -.0165  | .0046  | -.0314 |
| 22            | .808  | -.0100 | .2607  | .0283   | .0168  | -.0488 |



THREE-COMPONENT MEASUREMENTS OF A SERIES OF TAPERED WING  
(Elliptic Wing)

TABLE NO. 5 TO CHART 7

$$DE, \Lambda = \frac{4}{5}$$

| $\alpha^\circ$ | $c_a$   | $c_w$  | $c_M$   |
|----------------|---------|--------|---------|
| -5.66          | -0.1880 | 0.0144 | -0.0131 |
| 0              | 0       | .0053  | -.0001  |
| 5.77           | .1800   | .0144  | .0135   |
| 11.52          | .3750   | .0448  | .0181   |
| 17.27          | .5740   | .0982  | .0115   |
| 22.99          | .7940   | .1894  | -.0005  |
| 28.99          | 1.0050  | .3136  | -.0349  |
| 31.58          | 1.1020  | .4019  | -.0566  |
| 34.48          | 1.2030  | .5068  | -.0695  |
| 35.39          | 1.2750  | .6592  | -.0662  |
| 36.37          | 1.2890  | .6986  | -.0632  |
| 37.37          | 1.2950  | .7383  | -.0677  |
| 35.43          | 1.2450  | .5662  | -.0725  |
| 36.35          | 1.3080  | .6979  | -.0671  |
| 37.33          | 1.3220  | .7367  | -.0693  |
| 38.42          | 1.2540  | -      | -       |



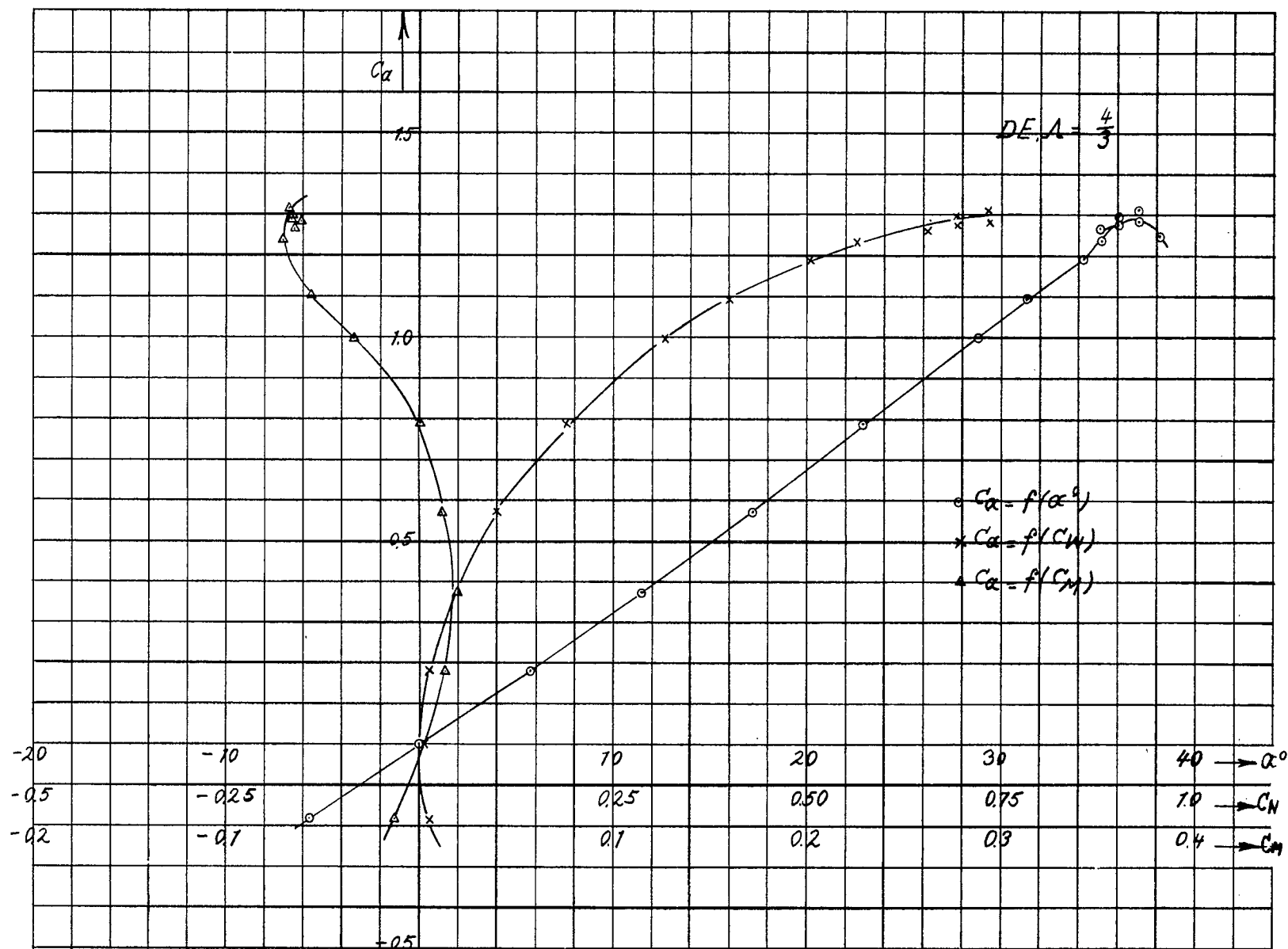


Chart 7. 3 - component measurements of a series of tapered wings (elliptic wing)  
Table 5.

## SIX-COMPONENT MEASUREMENTS OF A SERIES OF TAPERED WING

(Elliptic Wing)

TABLE NO. 6 TO CHARTS 8, 9

$$DE, \Lambda = \frac{4}{3}$$

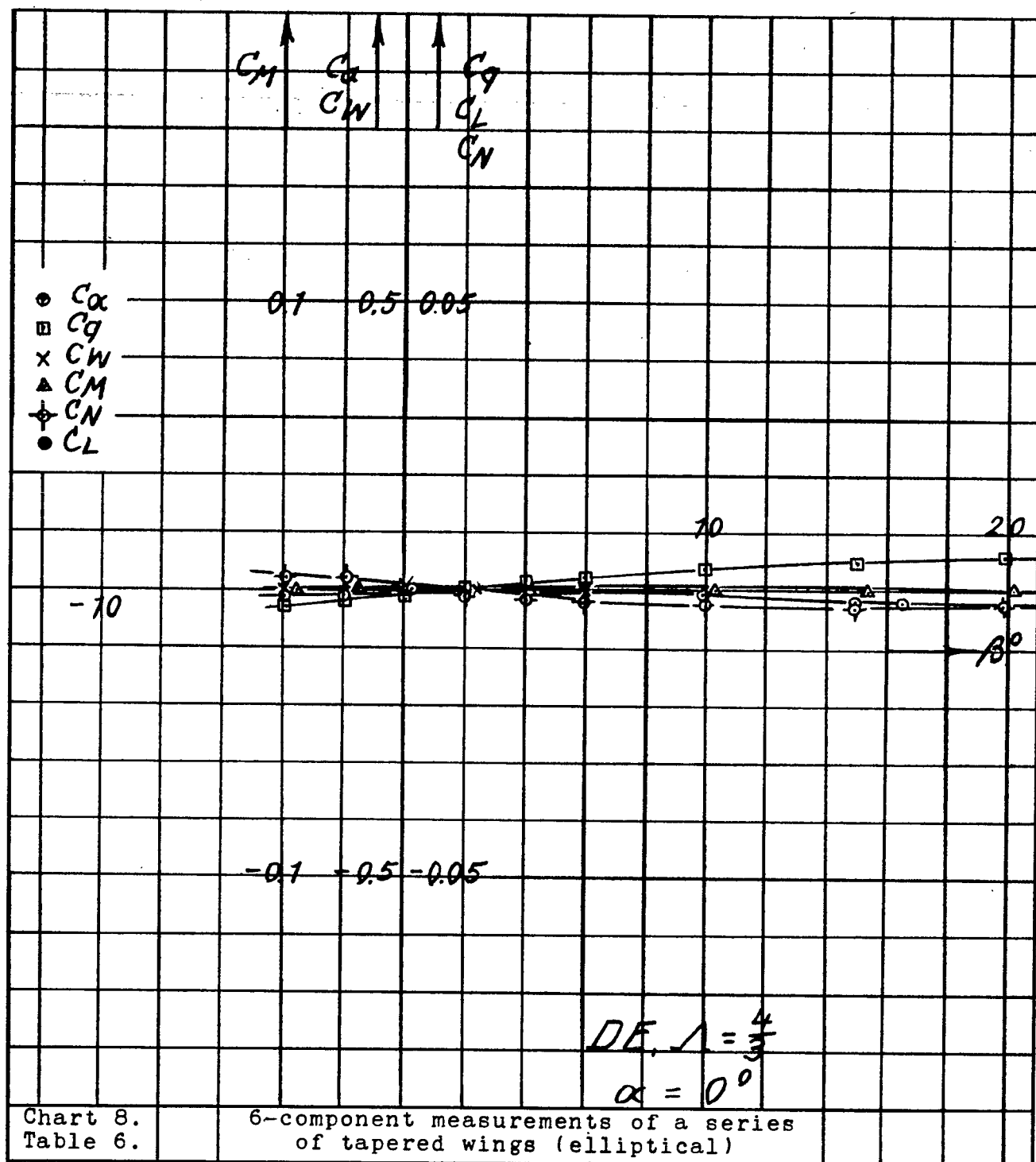
$$\alpha = 0$$

| $\beta^\circ$ | $c_a$   | $c_q$   | $c_w$  | $c_L$   | $c_M$  | $c_N$  |
|---------------|---------|---------|--------|---------|--------|--------|
| -4            | -0.0013 | -0.0027 | 0.0061 | -0.0010 | 0.0006 | 0.0024 |
| -2            | -.0013  | -.0020  | .0061  | -.0009  | .0006  | .0019  |
| 0             | -.0013  | -.0003  | .0060  | -.0005  | .0006  | .0001  |
| 2             | -.0013  | .0007   | .0060  | -.0004  | .0006  | -.0010 |
| 4             | -.0013  | .0020   | .0060  | -.0004  | .0006  | -.0018 |
| 6             | -.0013  | .0027   | .0065  | -.0004  | .0006  | -.0019 |
| 10            | -.0013  | .0040   | .0069  | .0002   | .0006  | -.0025 |
| 15            | -.0020  | .0053   | .0095  | .0004   | .0008  | -.0023 |
| 20            | -.0020  | .0066   | .0107  | .0005   | .0013  | -.0026 |

$$DE, \Lambda = \frac{4}{3}$$

$$\alpha = 9.43^\circ$$

| $\beta^\circ$ | $c_a$  | $c_q$   | $c_w$  | $c_L$   | $c_M$  | $c_N$  |
|---------------|--------|---------|--------|---------|--------|--------|
| -4            | 0.3040 | -0.0020 | 0.0316 | -0.0194 | 0.0147 | 0.0067 |
| -2            | .3025  | -.0020  | .0317  | -.0100  | .0153  | .0045  |
| 0             | .3040  | -.0020  | .0317  | .0002   | .0150  | .0014  |
| 2             | .3040  | -.0013  | .0317  | .0103   | .0152  | -.0017 |
| 4             | .3040  | -.0007  | .0317  | .0196   | .0148  | -.0039 |
| 6             | .3000  | -.0013  | .0316  | .0298   | .0156  | -.0054 |
| 10            | .2960  | -.0013  | .0317  | .0485   | .0143  | -.0092 |
| 15            | .2840  | -.0020  | .0315  | .0708   | .0134  | -.0138 |
| 20            | .2730  | -.0040  | .0320  | .0885   | .0106  | -.0158 |



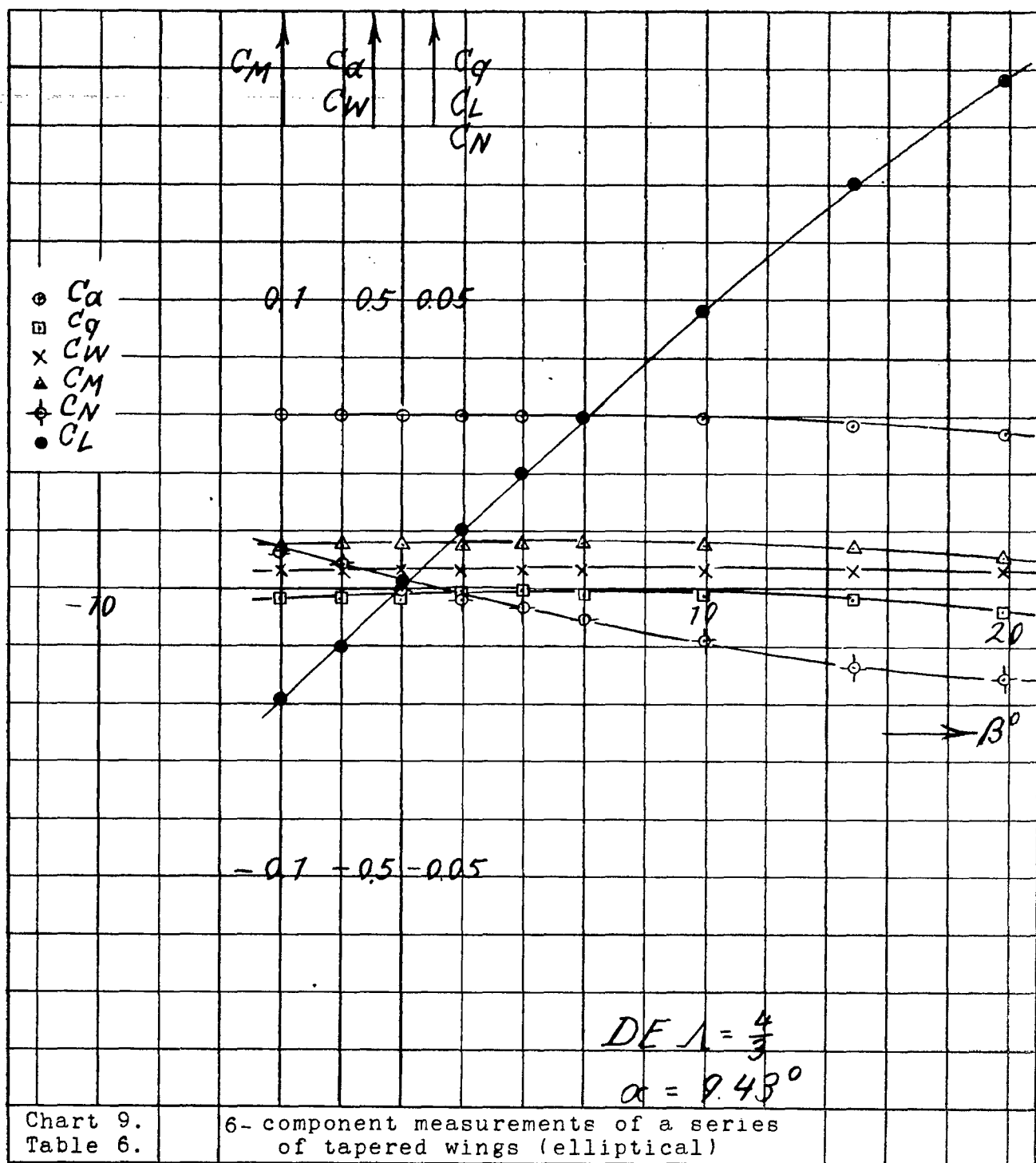


Chart 9.  
Table 6.

6-component measurements of a series  
of tapered wings (elliptical)

SIX-COMPONENT MEASUREMENTS OF A SERIES OF TAPERED WING  
(Elliptic Wing)

TABLE NO. 7 TO CHARTS 10, 11

$$DE, \Lambda = \frac{4}{3}$$

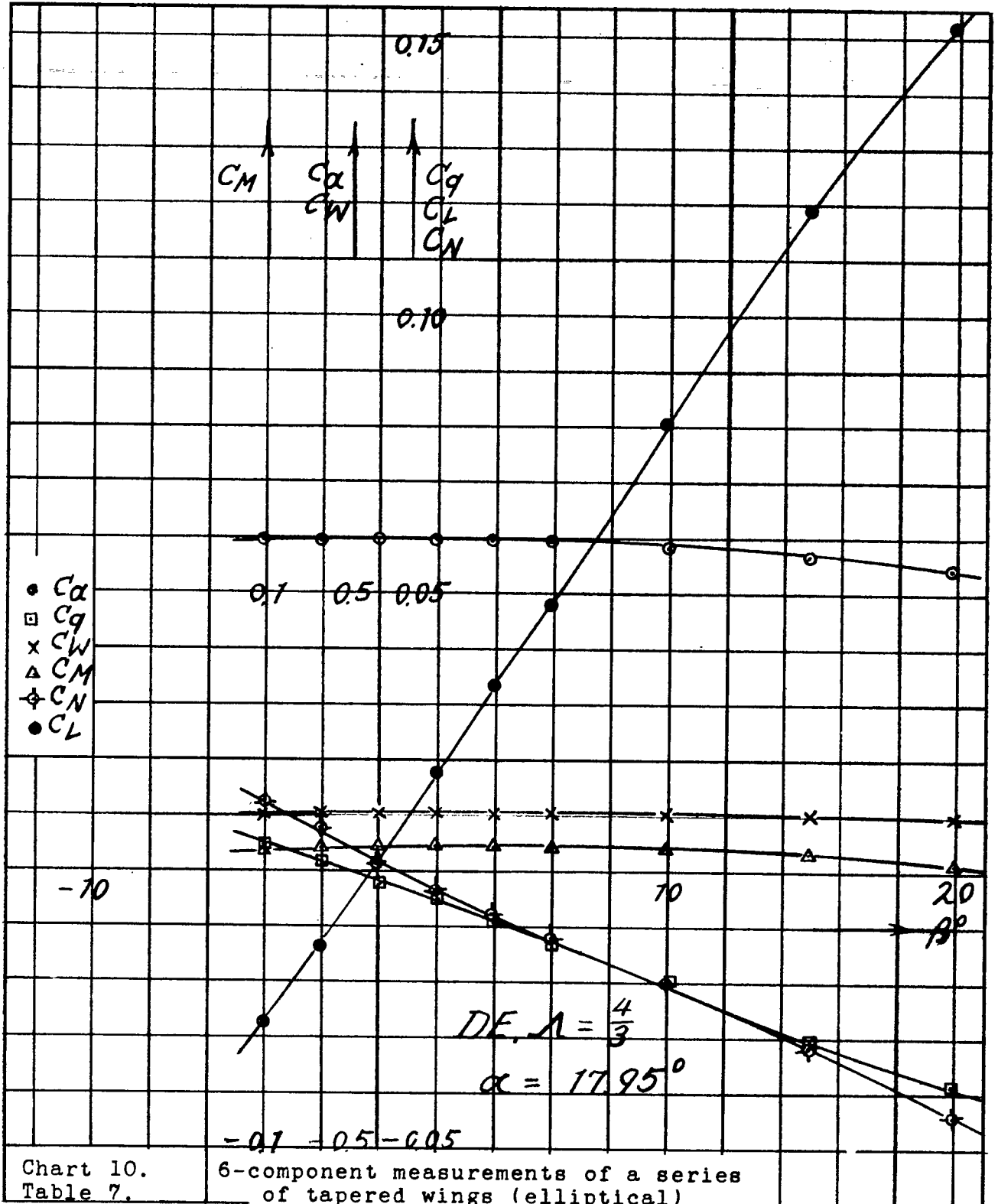
$$\alpha = 17.95^\circ$$

| $\beta^\circ$ | $c_a$  | $c_q$  | $c_w$  | $c_L$   | $c_M$  | $c_N$  |
|---------------|--------|--------|--------|---------|--------|--------|
| -4            | 0.6050 | 0.0050 | 0.1093 | -0.0277 | 0.0085 | 0.0124 |
| -2            | .6050  | .0020  | .1091  | -.0138  | .0086  | .0076  |
| 0             | .6050  | -.0020 | .1091  | .0022   | .0090  | .0015  |
| 2             | .6040  | -.0053 | .1080  | .0180   | .0097  | -.0039 |
| 4             | .6040  | -.0093 | .1076  | .0338   | .0088  | -.0081 |
| 6             | .6000  | -.0133 | .1076  | .0488   | .0083  | -.0123 |
| 10            | .5890  | -.0207 | .1051  | .0816   | .0080  | -.0211 |
| 15            | .5720  | -.0313 | .1012  | .1201   | .0060  | -.0326 |
| 20            | .5480  | -.0393 | .0985  | .1536   | .0025  | -.0450 |

$$DE, \Lambda = \frac{4}{3}$$

$$\alpha = 25.89^\circ$$

| $\beta^\circ$ | $c_a$  | $c_q$  | $c_w$  | $c_L$   | $c_M$   | $c_N$  |
|---------------|--------|--------|--------|---------|---------|--------|
| -4            | 0.9020 | 0.0213 | 0.2503 | -0.0397 | -0.0239 | 0.0184 |
| -2            | .9040  | .0107  | .2517  | -.0199  | -.0241  | .0124  |
| 0             | .9040  | 0      | .2520  | 0       | -.0241  | 0      |
| 2             | .9040  | -.0113 | .2510  | .0209   | -.0236  | -.0086 |
| 4             | .9030  | -.0227 | .2503  | .0391   | -.0241  | -.0149 |
| 6             | .8940  | -.0327 | .2474  | .0580   | -.0228  | -.0235 |
| 10            | .8740  | -.0533 | .2412  | .0932   | -.0197  | -.0372 |
| 15            | .8580  | -.0660 | .2459  | .1334   | -.0203  | -.0685 |
| 20            | .8140  | -.0707 | .2440  | .1510   | -.0205  | -.0889 |



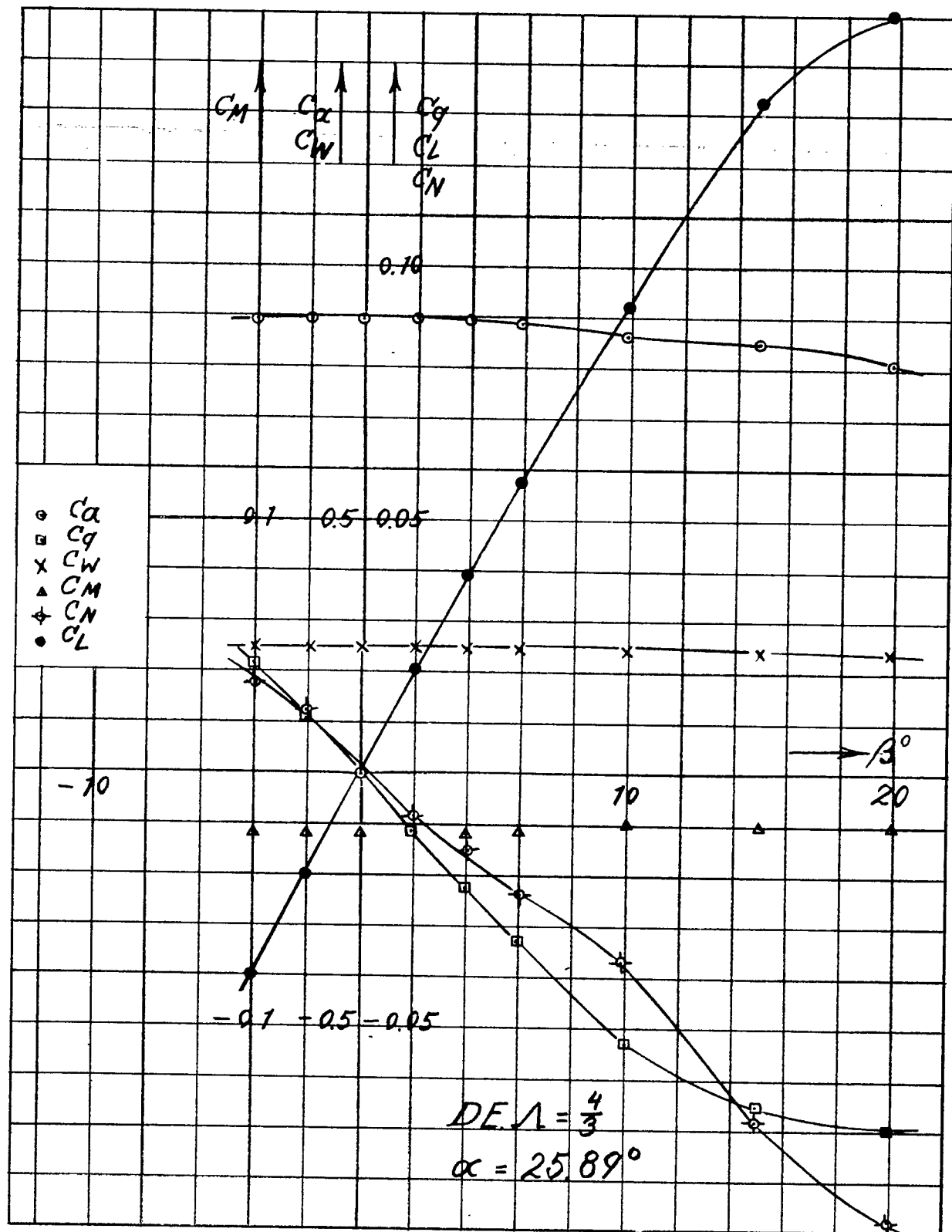


Chart 11.

6 - component measurements of a series of tapered wings (elliptic wing)

Table 7.

SIX-COMPONENT MEASUREMENTS OF A SERIES OF TAPERED WING  
(Elliptic Wing)

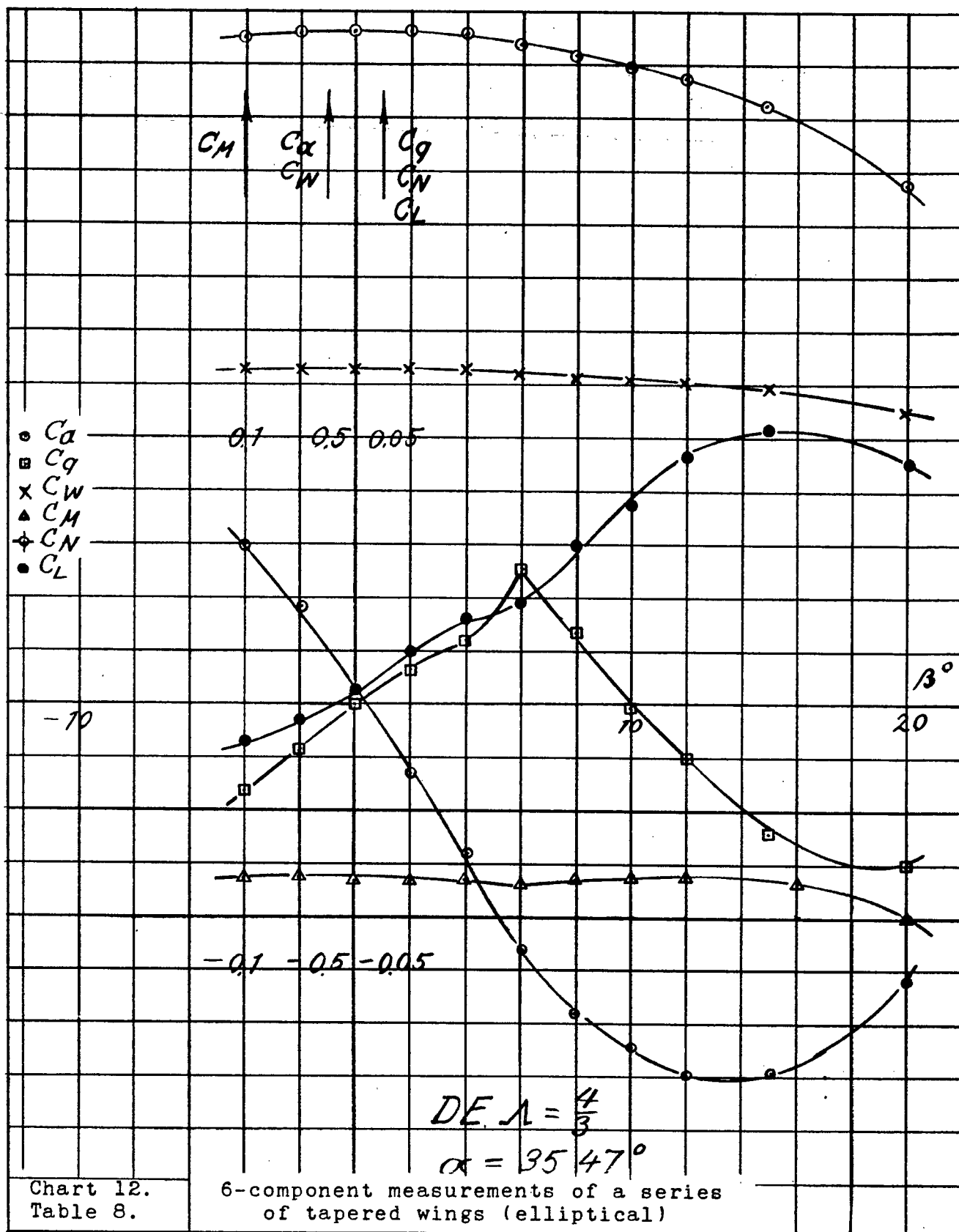
TABLE NO. 8 TO CHART 12

$$DE, \Lambda = \frac{4}{3}$$

$$\alpha = 35.47^\circ$$

| $\beta^\circ$ | $c_a$  | $c_q$   | $c_w$  | $c_L$   | $c_M$   | $c_N$  |
|---------------|--------|---------|--------|---------|---------|--------|
| -4            | 1.2680 | -0.0167 | 0.6387 | -0.0074 | -0.0662 | 0.0300 |
| -2            | 1.2780 | -.0087  | .6355  | -.0036  | -.0659  | .0183  |
| 0             | 1.2740 | 0       | .6327  | .0019   | -.0667  | .0028  |
| 2             | 1.2790 | .0067   | .6382  | .0096   | -.0669  | -.0133 |
| 4             | 1.2710 | .0120   | .6369  | .0159   | -.0667  | -.0284 |
| 6             | 1.2540 | .0253   | .6234  | .0189   | -.0692  | -.0467 |
| 8             | 1.2310 | .0133   | .6198  | .0299   | -.0670  | -.0593 |
| 10            | 1.2110 | -.0013  | .6194  | .0378   | -.0663  | -.0655 |
| 12            | 1.1880 | -.0100  | .6127  | .0465   | -.0664  | -.0719 |
| 15            | 1.1330 | -.0247  | .5982  | .0519   | -.0688  | -.0718 |
| 20            | .9840  | -.0307  | .5537  | .0453   | -.0824  | -.0561 |





## THREE-COMPONENT MEASUREMENTS OF A SERIES OF TAPERED WING

(Elliptic Wing)

TABLE NO. 9 TO CHART 13

 $CE, \Lambda = 1$ 

| $\alpha^\circ$ | $c_a$   | $c_w$  | $c_M$   |
|----------------|---------|--------|---------|
| -5.80          | -0.1600 | 0.0159 | -0.0077 |
| .01            | -.0080  | .0060  | -.0006  |
| 5.83           | .1386   | .0137  | .0104   |
| 11.63          | .2959   | .0393  | .0111   |
| 17.41          | .4691   | .0886  | 0       |
| 23.16          | .6612   | .1748  | -.0284  |
| 28.92          | .8600   | .3059  | -.0664  |
| 31.81          | .9465   | .3826  | -.0847  |
| 34.72          | 1.0160  | .4703  | -.0992  |
| 35.69          | 1.0440  | .5017  | -.1081  |
| 36.65          | 1.0710  | .5348  | -.1139  |
| 37.62          | 1.0930  | .5677  | -.1190  |
| 38.60          | 1.1110  | .5991  | -.1252  |
| 39.40          | 1.1270  | .6326  | -.1314  |
| 40.56          | 1.1440  | .6747  | -.1371  |

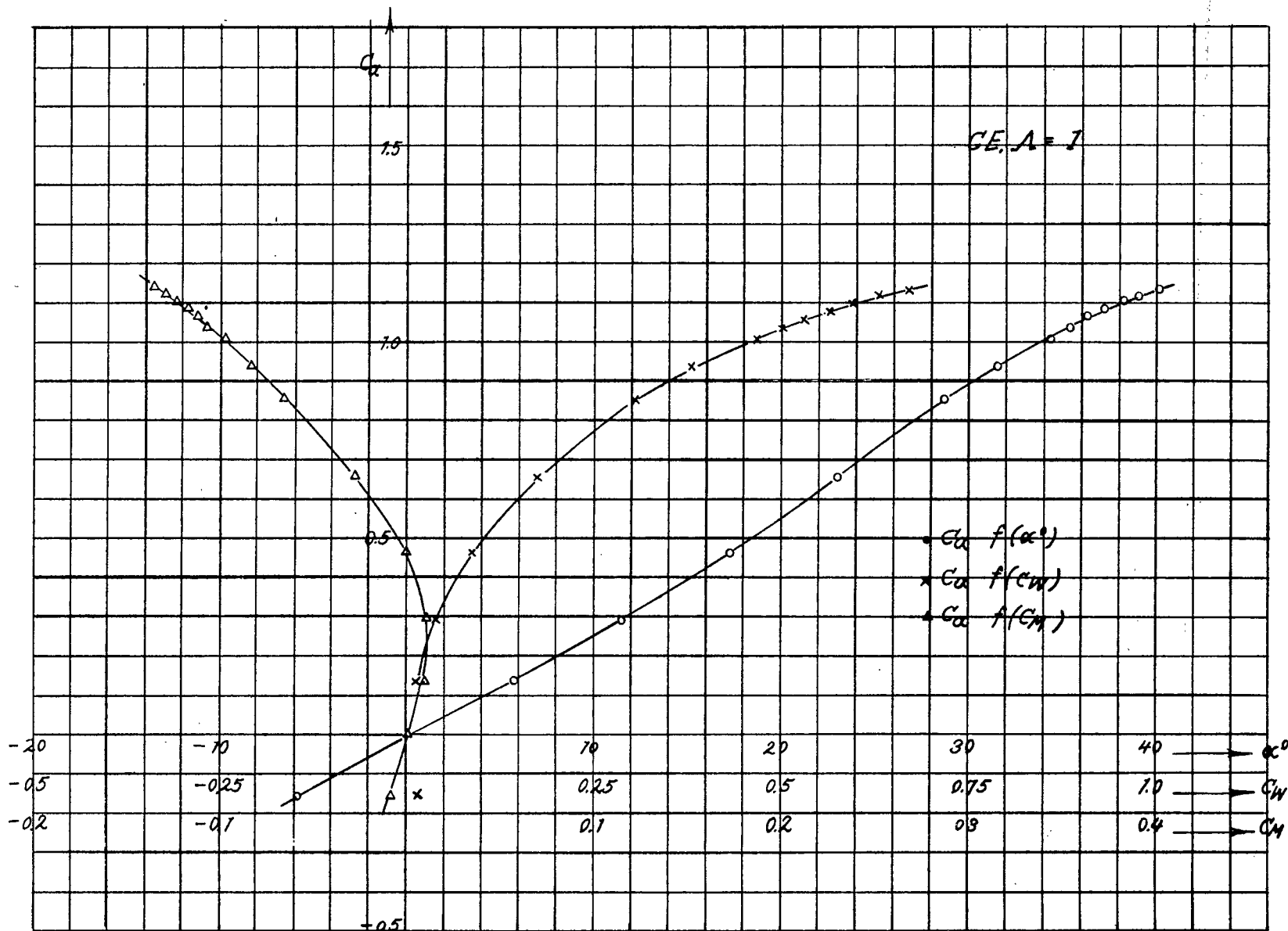


Chart 13. 3 - component measurements of a series of tapered wings (elliptic wing)  
Table 9

SIX-COMPONENT MEASUREMENTS OF A SERIES OF TAPERED WING  
(Elliptic Wing)

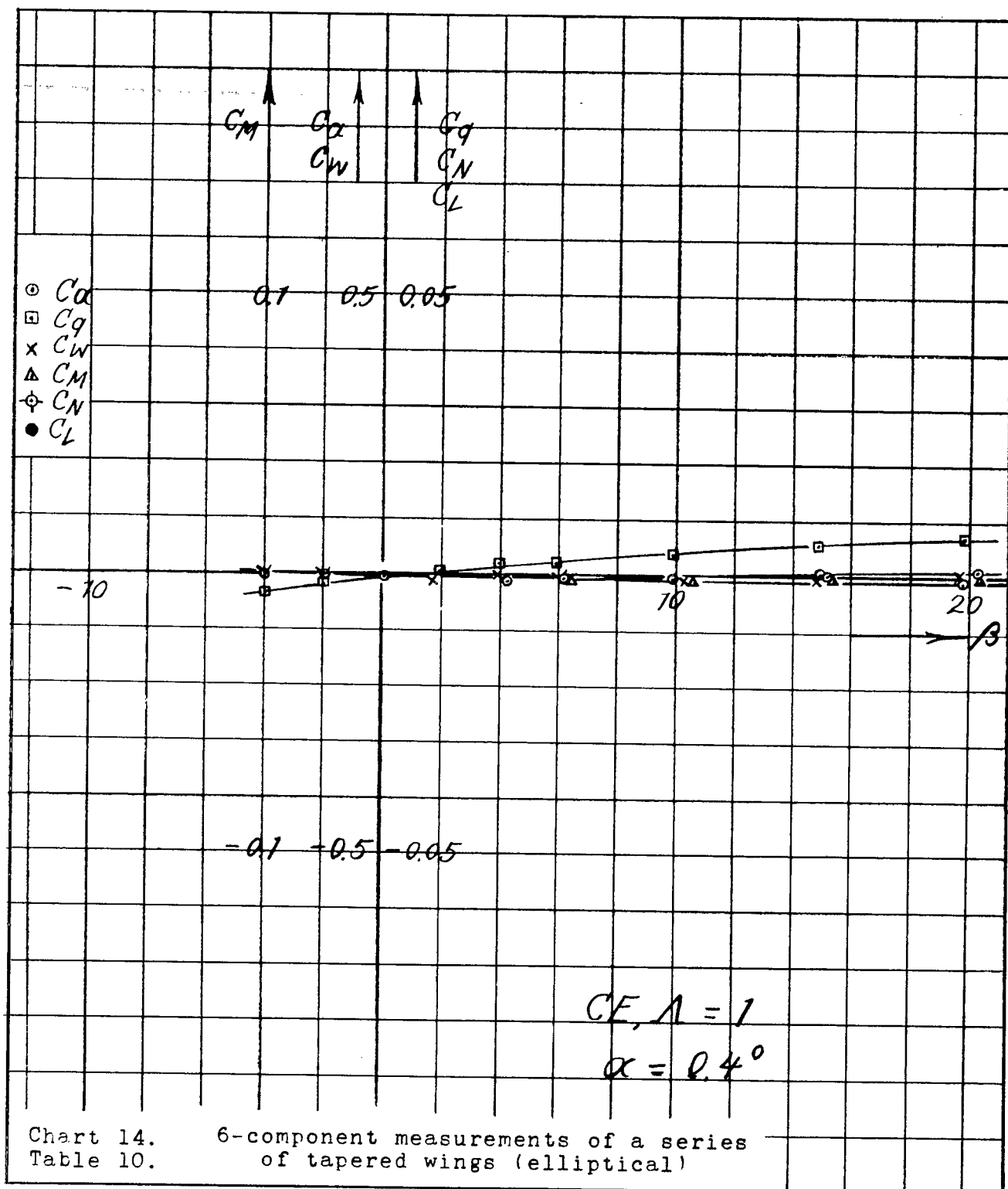
TABLE NO. 10 TO CHARTS 14, 15

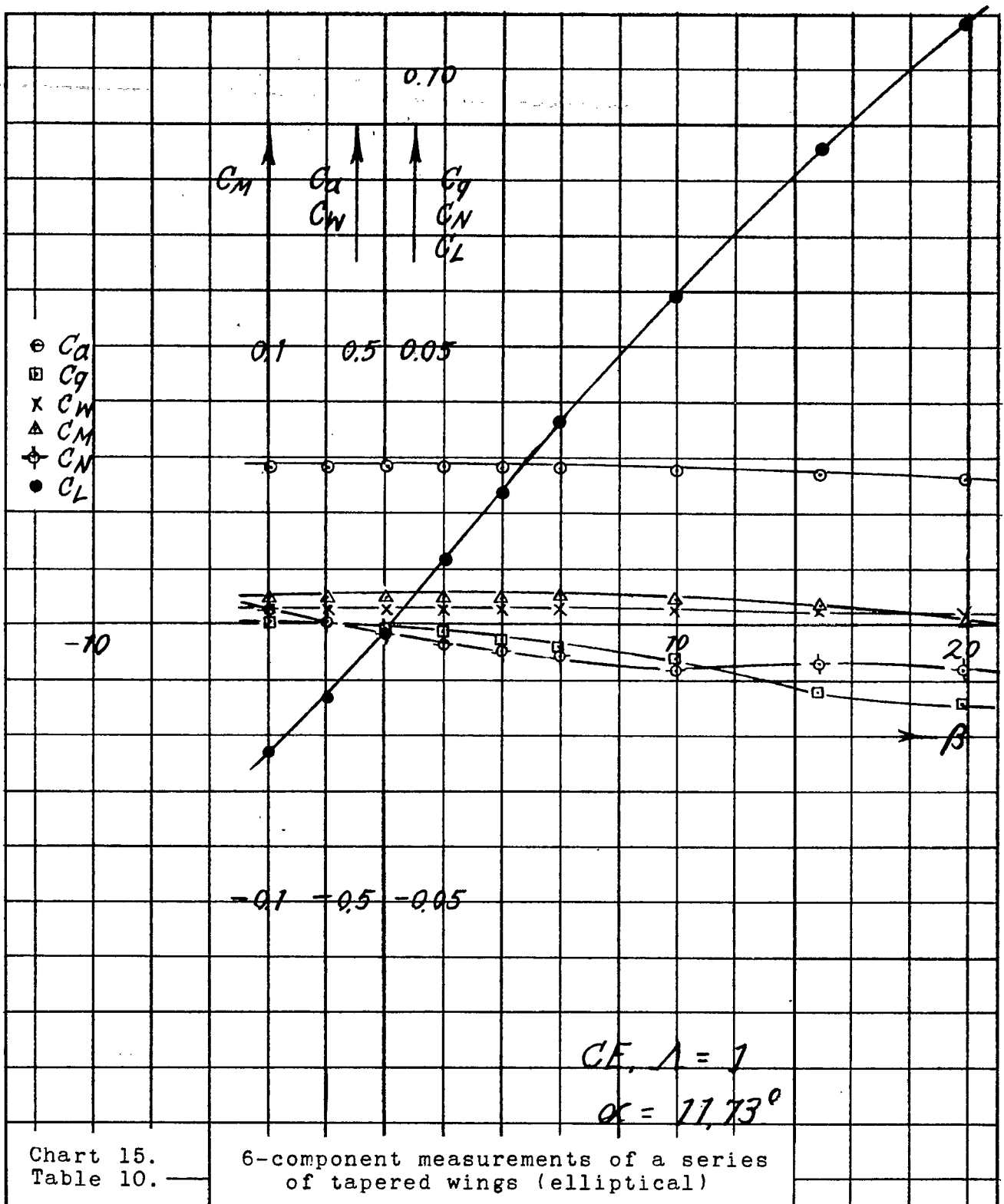
CE,  $\Lambda = 1$  $\alpha = 0.4^\circ$ 

| $\beta^\circ$ | $c_a$  | $c_q$   | $c_w$  | $c_L$   | $c_M$   | $c_N$  |
|---------------|--------|---------|--------|---------|---------|--------|
| -4            | 0.0013 | -0.0033 | 0.0067 | -0.0001 | -0.0044 | 0.0014 |
| -2            | .0013  | -.0013  | .0061  | 0       | -.0046  | .0002  |
| 0             | .0013  | 0       | .0060  | 0       | -.0046  | -.0002 |
| 2             | .0013  | .0013   | .0063  | 0       | -.0046  | -.0006 |
| 4             | .0013  | .0027   | .0065  | .0001   | -.0046  | -.0009 |
| 6             | .0013  | .0027   | .0069  | .0002   | -.0045  | .0001  |
| 10            | .0013  | .0040   | .0083  | .0002   | -.0045  | .0011  |
| 15            | .0013  | .0067   | .0093  | .0015   | -.0045  | .0015  |
| 20            | .0013  | .0080   | .0108  | .0016   | -.0045  | .0029  |

CE,  $\Lambda = 1$  $\alpha = 11.73^\circ$ 

| $\beta^\circ$ | $c_a$  | $c_q$  | $c_w$  | $c_L$   | $c_M$  | $c_N$  |
|---------------|--------|--------|--------|---------|--------|--------|
| -4            | 0.2974 | 0.0013 | 0.0393 | -0.0226 | 0.0111 | 0.0038 |
| -2            | 0.2974 | .0007  | .0391  | -.0129  | .0119  | .0014  |
| 0             | .2974  | 0      | .0391  | 0       | .0116  | -.0006 |
| 2             | .2974  | -.0007 | .0388  | .0129   | .0113  | -.0030 |
| 4             | .2960  | -.0020 | .0391  | .0248   | .0117  | -.0037 |
| 6             | .2935  | -.0033 | .0388  | .0378   | .0122  | -.0047 |
| 10            | .2908  | -.0053 | .0391  | .0605   | .0109  | -.0072 |
| 15            | .2855  | -.0113 | .0395  | .0878   | .0086  | -.0061 |
| 20            | .2800  | -.0133 | .0383  | .1103   | .0044  | -.0070 |





SIX-COMPONENT MEASUREMENTS OF A SERIES OF TAPERED WING  
(Elliptic Wing)

TABLE NO. 11 TO CHARTS 16, 17

$$CE, \Lambda = 1$$

$$\alpha = 21.36^\circ$$

| $\beta^\circ$ | $c_a$  | $c_q$  | $c_w$  | $c_L$   | $c_M$   | $c_N$  |
|---------------|--------|--------|--------|---------|---------|--------|
| -4            | 0.5960 | 0.0113 | 0.1429 | -0.0327 | -0.0185 | 0.0082 |
| -2            | .5980  | .0047  | .1436  | -.0128  | -.0181  | .0040  |
| 0             | .6000  | -.0013 | .1435  | .0025   | -.0190  | .0003  |
| 2             | .5990  | -.0060 | .1433  | .0153   | -.0182  | -.0044 |
| 4             | .5980  | -.0120 | .1423  | .0340   | -.0188  | -.0085 |
| 6             | .5960  | -.0207 | .1416  | .0544   | -.0190  | -.0118 |
| 10            | .5850  | -.0374 | .1367  | .0982   | -.0173  | -.0169 |
| 15            | .5740  | -.0588 | .1312  | .1469   | -.0189  | -.0236 |
| 20            | .5660  | -.0781 | .1273  | .1854   | -.0220  | -.0334 |

$$CE, \Lambda = 1$$

$$\alpha = 30.3^\circ$$

| $\beta^\circ$ | $c_a$  | $c_q$  | $c_w$  | $c_L$   | $c_M$   | $c_N$  |
|---------------|--------|--------|--------|---------|---------|--------|
| -4            | 0.8920 | 0.0280 | 0.3383 | -0.0445 | -0.0718 | 0.0229 |
| -2            | .8940  | .0120  | .3424  | -.0226  | -.0732  | .0137  |
| 0             | .8990  | -.0053 | .3422  | .0017   | -.0744  | .0019  |
| 2             | .8990  | -.0213 | .3412  | .0256   | -.0742  | -.0076 |
| 4             | .8930  | -.0380 | .3374  | .0510   | -.0717  | -.0153 |
| 6             | .8860  | -.0513 | .3309  | .0709   | -.0691  | -.0254 |
| 10            | .8750  | -.0860 | .3221  | .1169   | -.0675  | -.0372 |
| 15            | .8330  | -.1159 | .2987  | .1758   | -.0612  | -.0626 |
| 20            | .8000  | -.1431 | .2799  | .2259   | -.0610  | -.0835 |

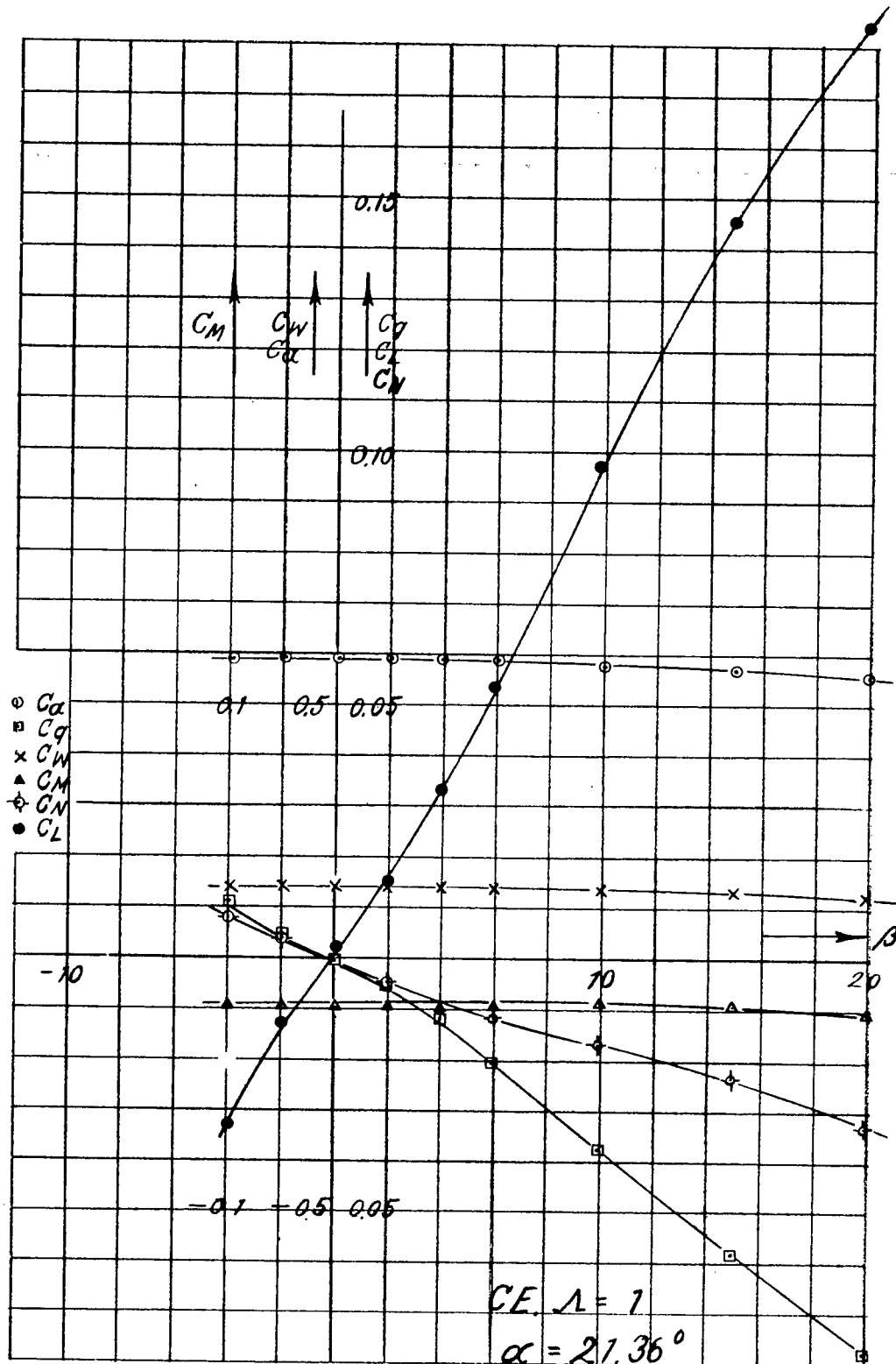


Chart 16.

6 - component measurements of a series of tapered wings (elliptic wing)

Table 11.



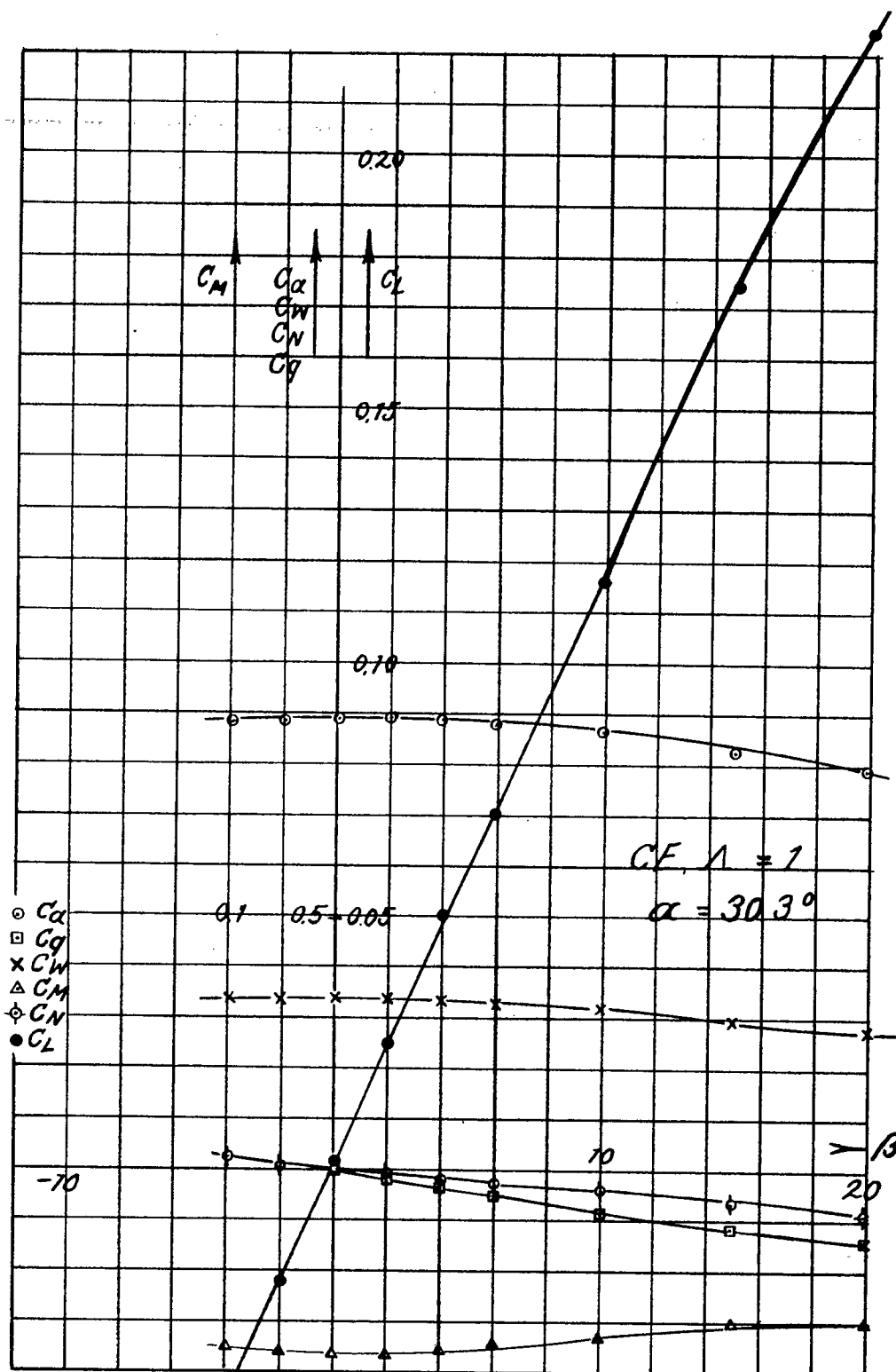


Chart 17.  
Table 11.

6 - component measurements of a series of tapered wings (elliptic wing)

SIX-COMPONENT MEASUREMENTS OF A SERIES OF TAPERED WING  
(Elliptic Wing)

TABLE NO. 12 TO CHART 18

 $CE, \Lambda = 1$  $\alpha = 38.63^\circ$ 

| $\beta^\circ$ | $c_a$  | $c_q$  | $c_w$  | $c_L$   | $c_M$   | $c_N$  |
|---------------|--------|--------|--------|---------|---------|--------|
| -4            | 1.1110 | 0.0394 | 0.6028 | -0.0387 | -0.1260 | 0.0357 |
| -2            | 1.1110 | .0167  | .6053  | -.0198  | -.1263  | .0203  |
| 0             | 1.1150 | -.0040 | .6042  | .0015   | -.1266  | .0014  |
| 2             | 1.1130 | -.0254 | .6037  | .0232   | -.1267  | -.0135 |
| 4             | 1.1090 | -.0487 | .5989  | .0435   | -.1264  | -.0285 |
| 6             | 1.1050 | -.0720 | .5921  | .0650   | -.1247  | -.0412 |
| 10            | 1.0790 | -.1167 | .5724  | .1027   | -.1181  | -.0634 |
| 15            | 1.0370 | -.1620 | .5454  | .1522   | -.1104  | -.0976 |
| 20            | .9830  | -.2066 | .5087  | .1927   | -.1028  | -.1191 |

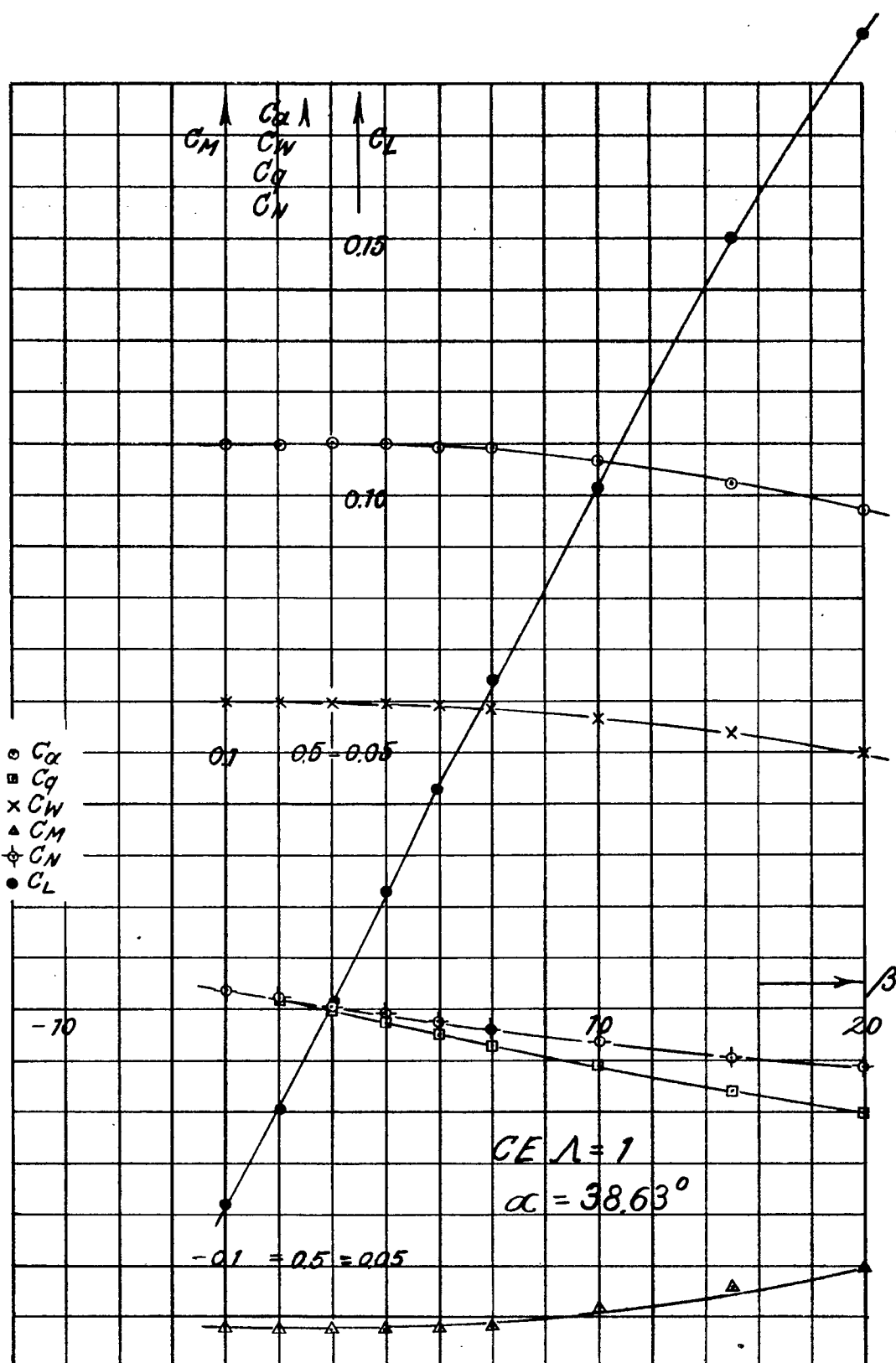


Chart 18.

6 - component measurements of a series of tapered wings (elliptic wing)

Table 17.

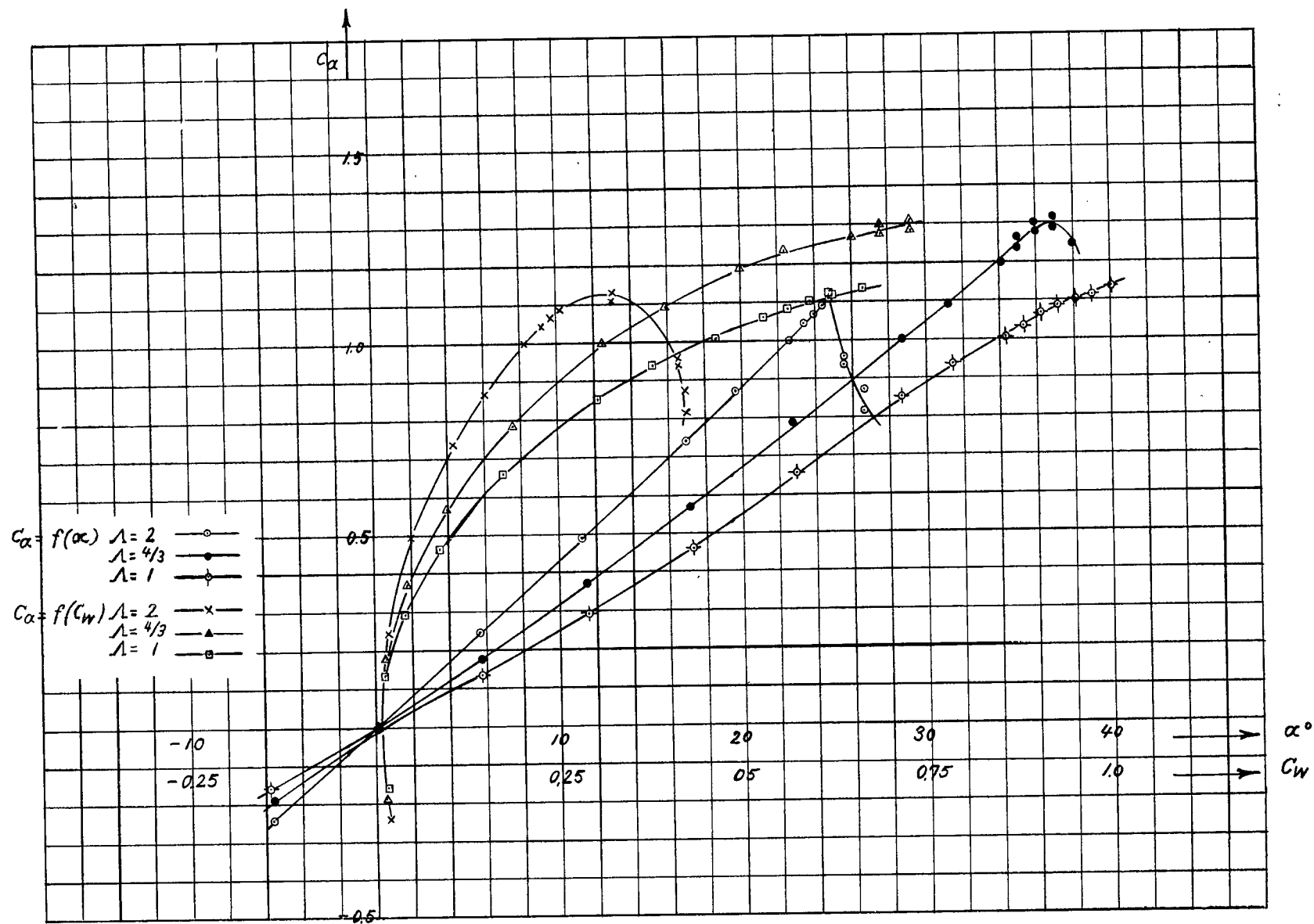
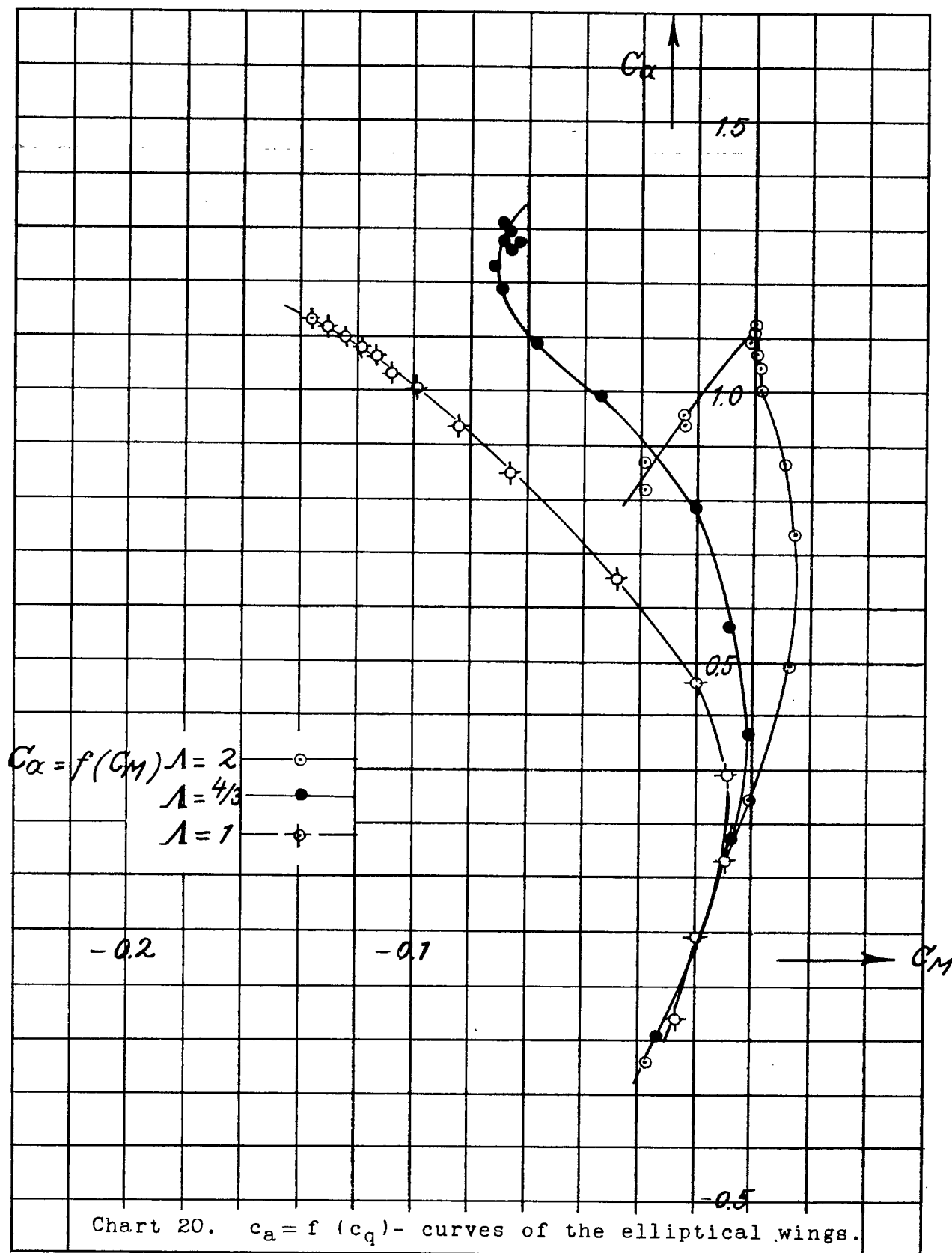
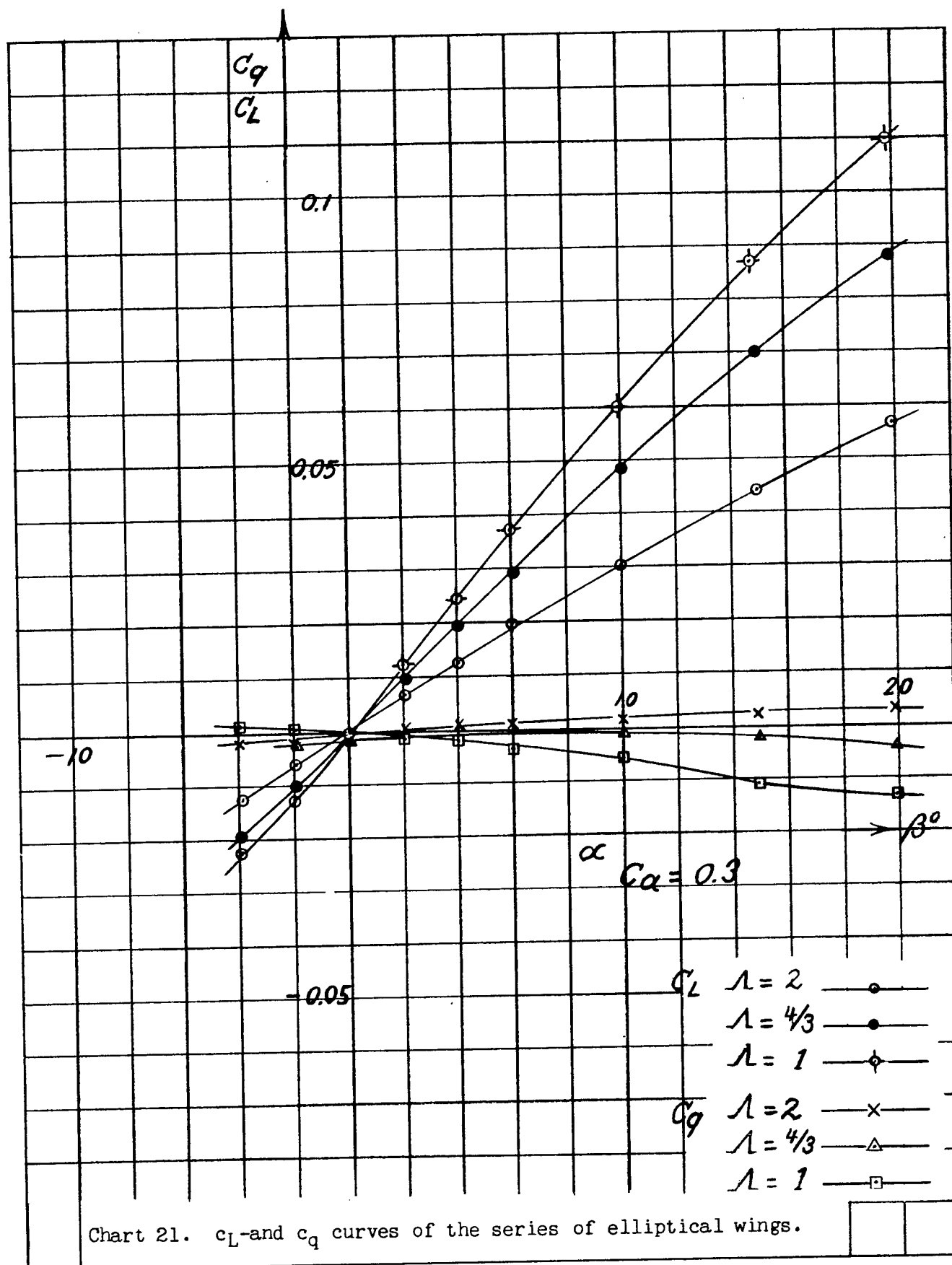
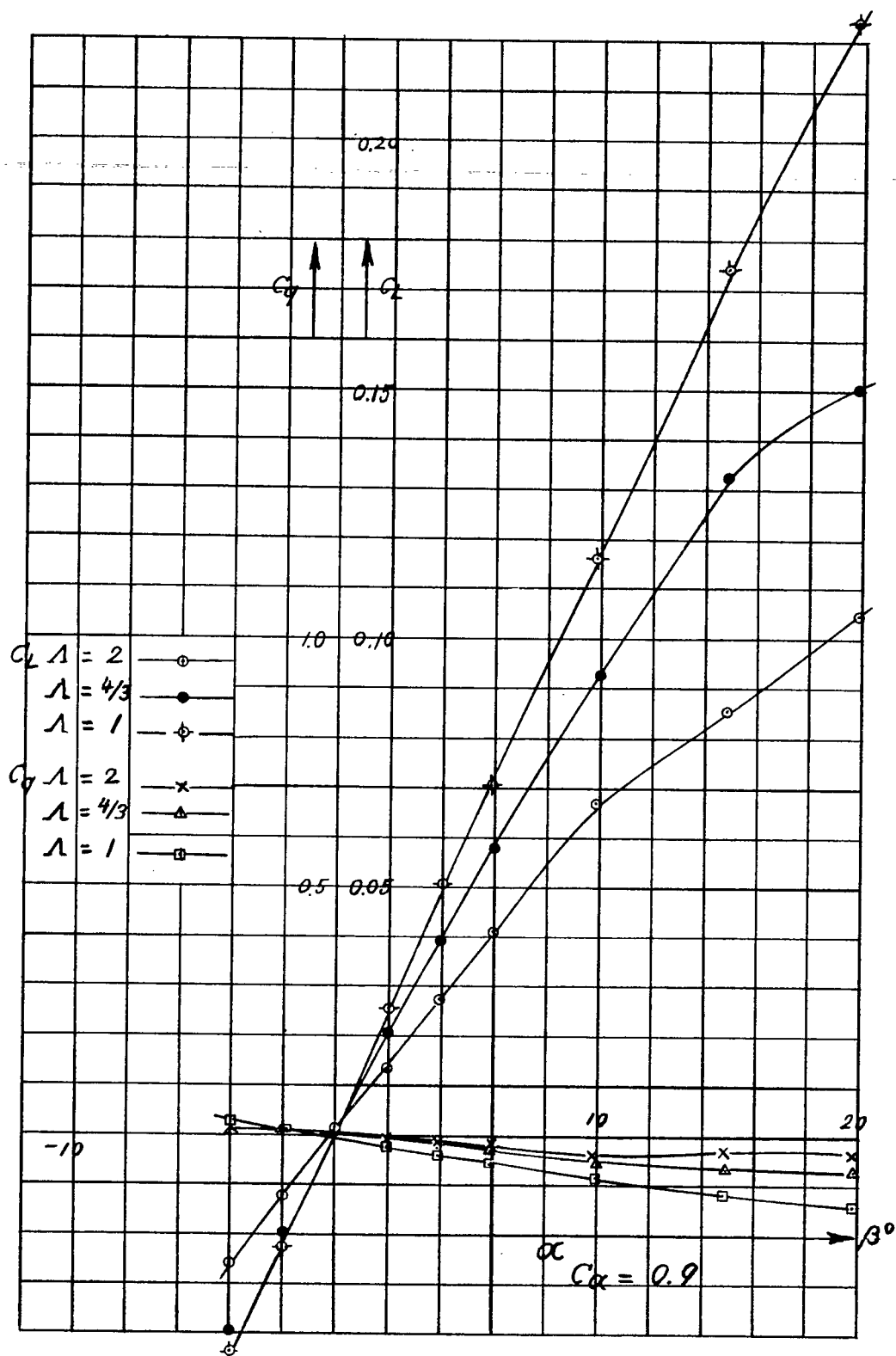


Chart 19.  $c_a = f(\alpha)$  - and  $c_a = f(c_w)$  - curves of the series of elliptic wings.



Chart 21.  $c_L$ -and  $c_q$  curves of the series of elliptical wings.

Chart 22.  $c_L$ - and  $c_q$ - curves of the series of elliptic wings.

NASA Technical Library



3 1176 01437 4533